

# Planets in Protoplanetary Disks: Dynamical Processes and Observational Prospects

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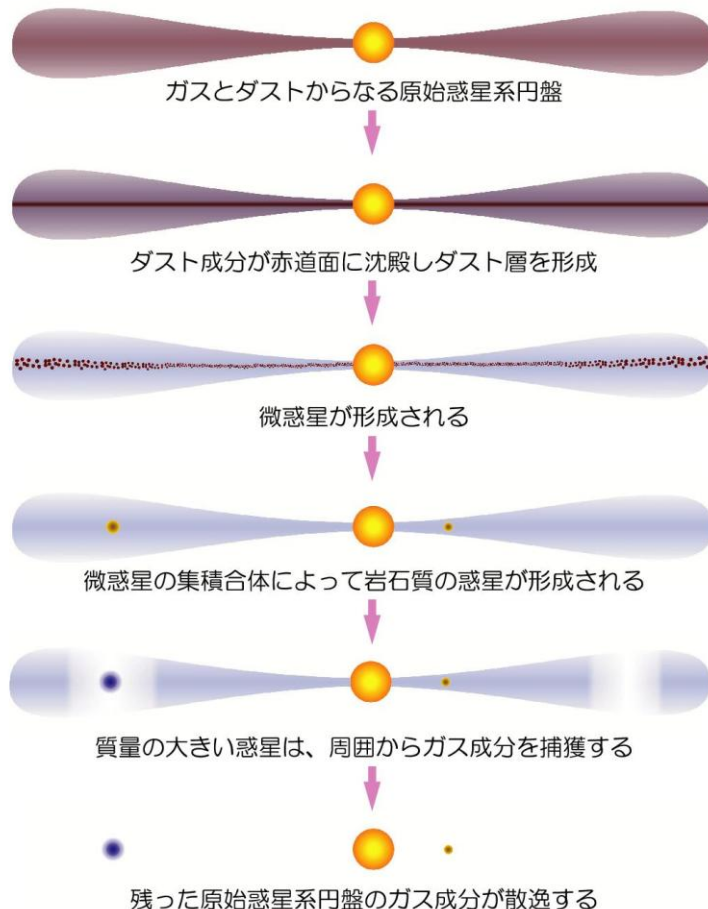
# Outline

- Introduction: Planet Formation and Disk-Planet Interaction
- Spiral Density Wave Theory and Type I Planet Migration
- Direct Imaging Observations of Disk Non-axisymmetric Structures

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# Planet Formation Scenario

## 惑星系形成の標準的なシナリオ（京都モデル）



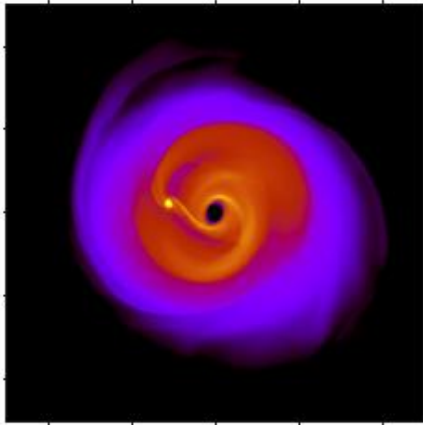
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- Initial condition:
  - Protoplanetary disk
  - Mixture of gas and dust particles ( $\sim 1\mu\text{m}$ )
- Coagulation of dust particles in the disk
  - Planetesimals ( $\sim 1\text{km}$ )
  - Protoplanets ( $\sim 1000\text{km}$ )
- Disk gas dispersal
- Disk lifetime  $\sim 10^{6-7}$  yr
  - Timescale constraint on (gaseous) planet formation

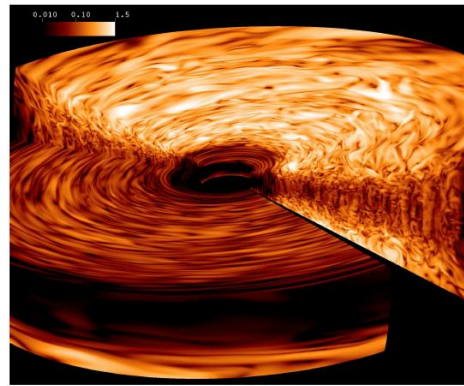
# Dynamical Processes in Protoplanetary Disks

Turbulence:

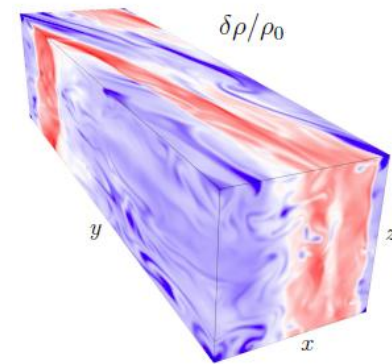
gravitational instability / magnetorotational instability / others...



Boley 2009

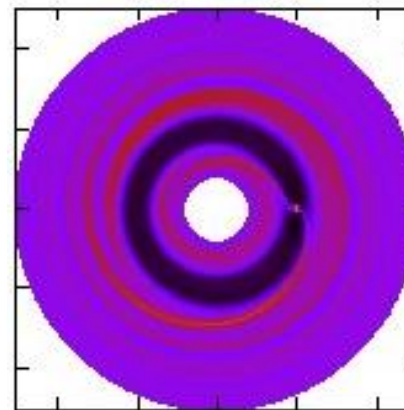
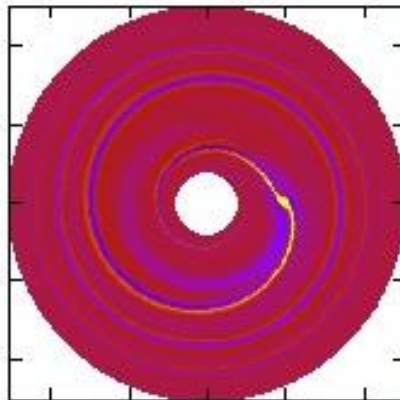


Flock et al. 2011



Heinemann and Papaloizou 2009

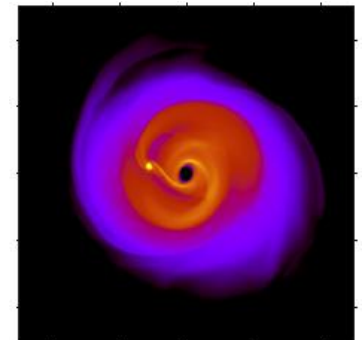
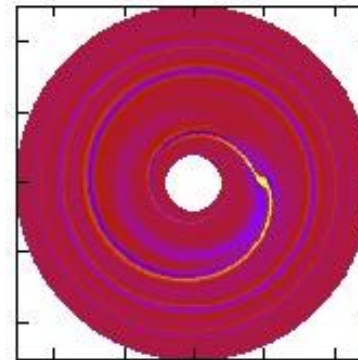
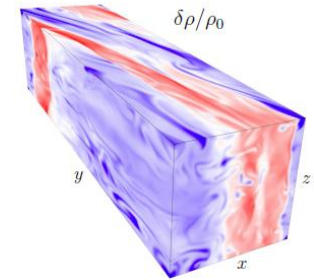
Disk-planet interaction: spiral wave, gap-opening...



FARGO simulation

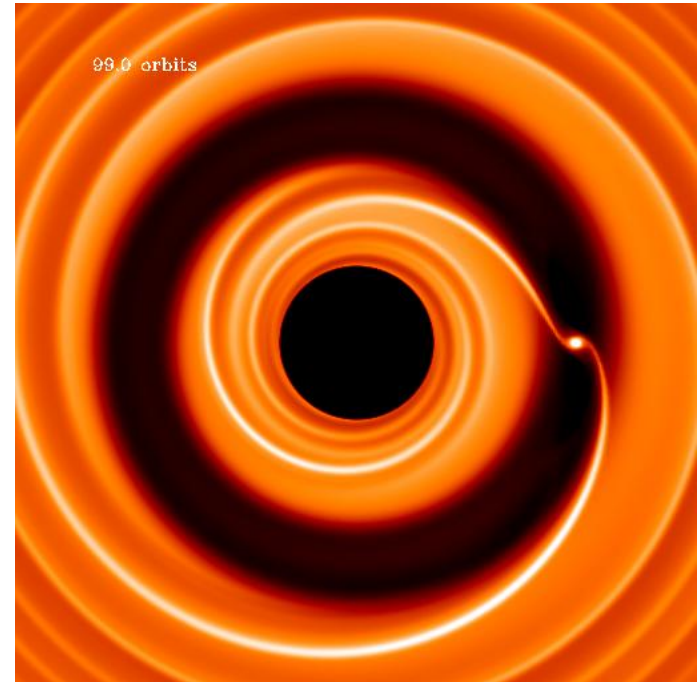
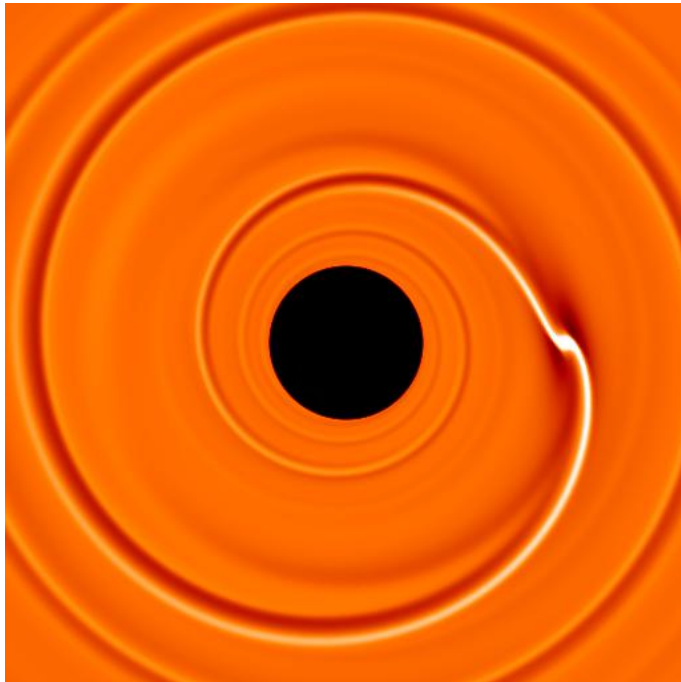
# Spiral Wave as an Indicator of Dynamical Activity in a Disk

- Spiral structures are expected quite generally in dynamically active disks
- Spiral density wave
  - (non-axisymmetric) sound wave excited in a disk
  - Any perturbation can cause non-axisymmetric structures



# Disk-Planet Interaction

- Gravitational Interaction between a Planet and a Disk
  - And nothing more...

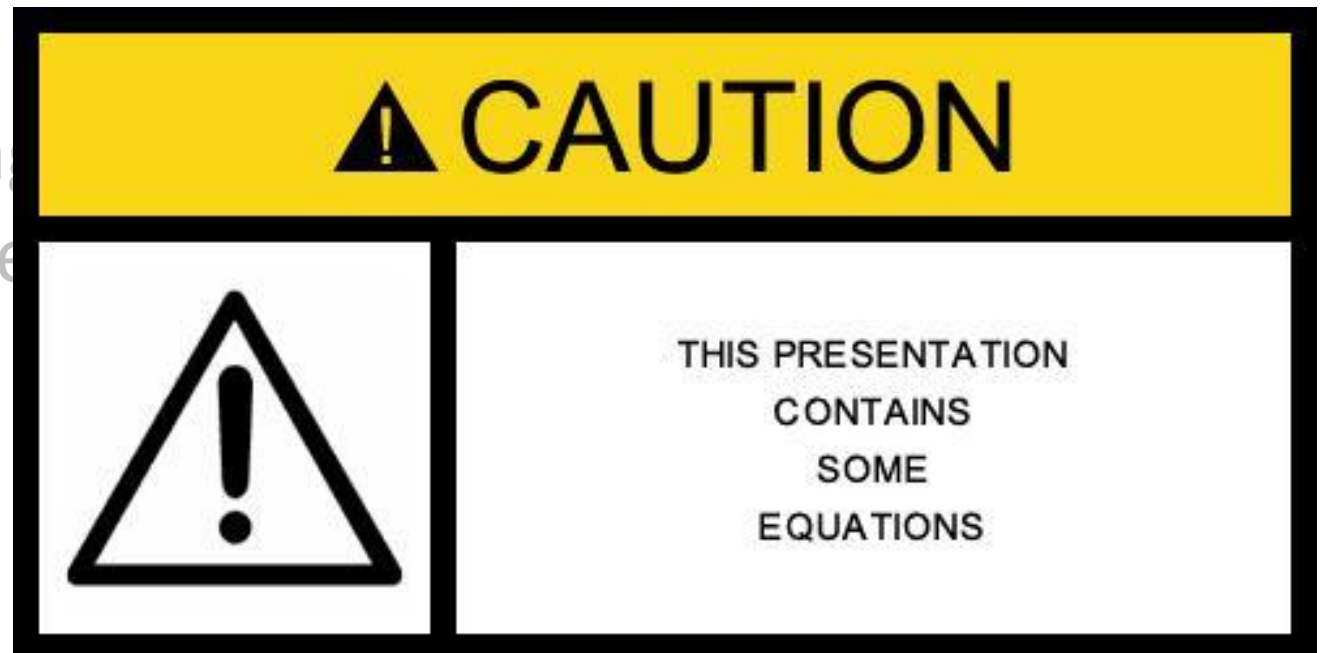


# Why Disk-Planet Interaction?

- Radial migration of the planet
  - Planets can migrate significantly before the dispersal of the gas disk
  - Impact on planet formation theory
- Redistribution of the gas in the disk
  - Planets can form a spiral density wave, gap, possibly inner hole...
  - Observational predictions



- Introduction: Planet Formation and Disk-Planet Interaction
- **Spiral Density Wave Theory and Type I Planet Migration**
- Direct Imaging of Exoplanets  
axisymmetric

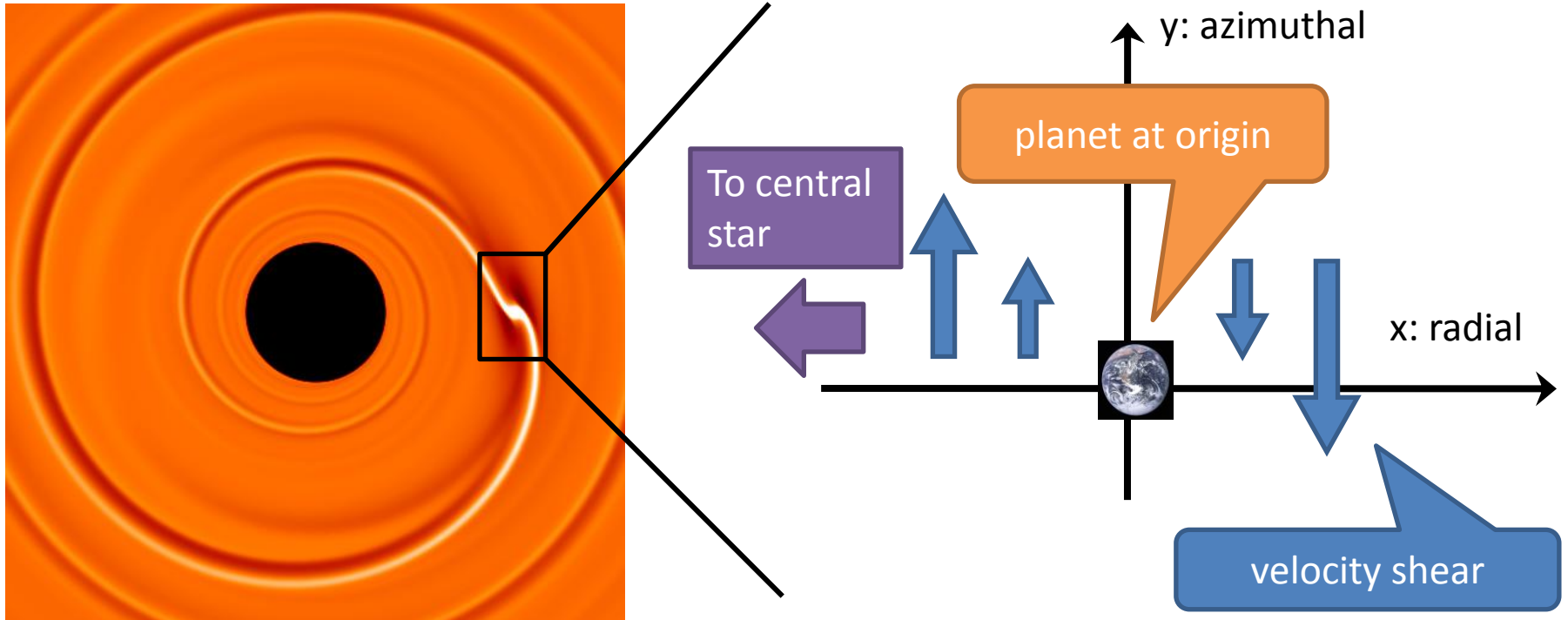


# Problem Setup

- Consider the simplest case
  - A planet in a circular orbit in a circular disk
- We expect a steady state ***in a rotating frame with the planet***

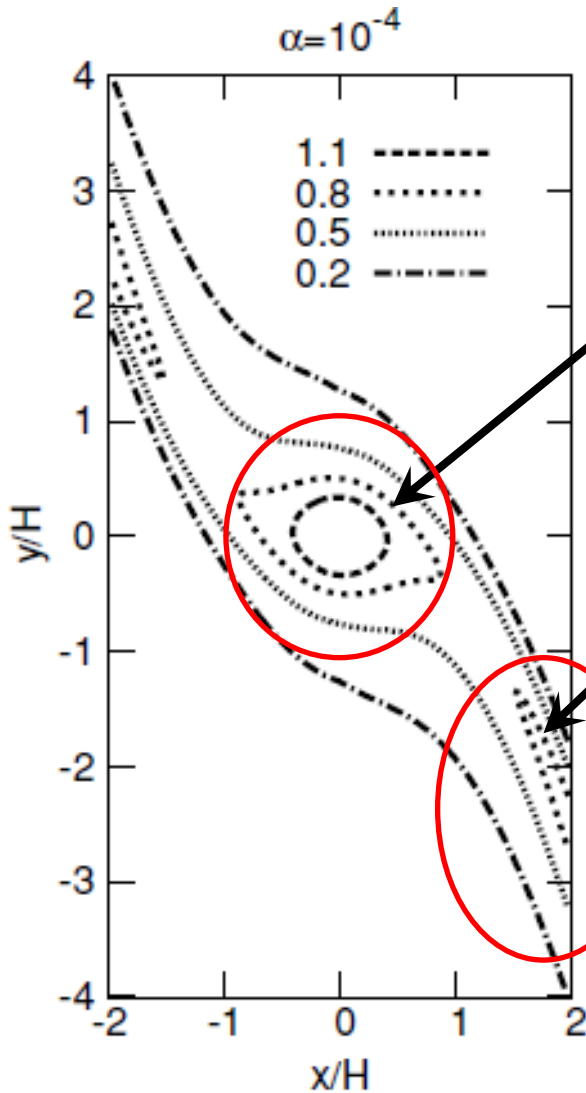


# Shearing-sheet close-up view around the planet



$$v_y = -\frac{3}{2}\Omega_p x$$

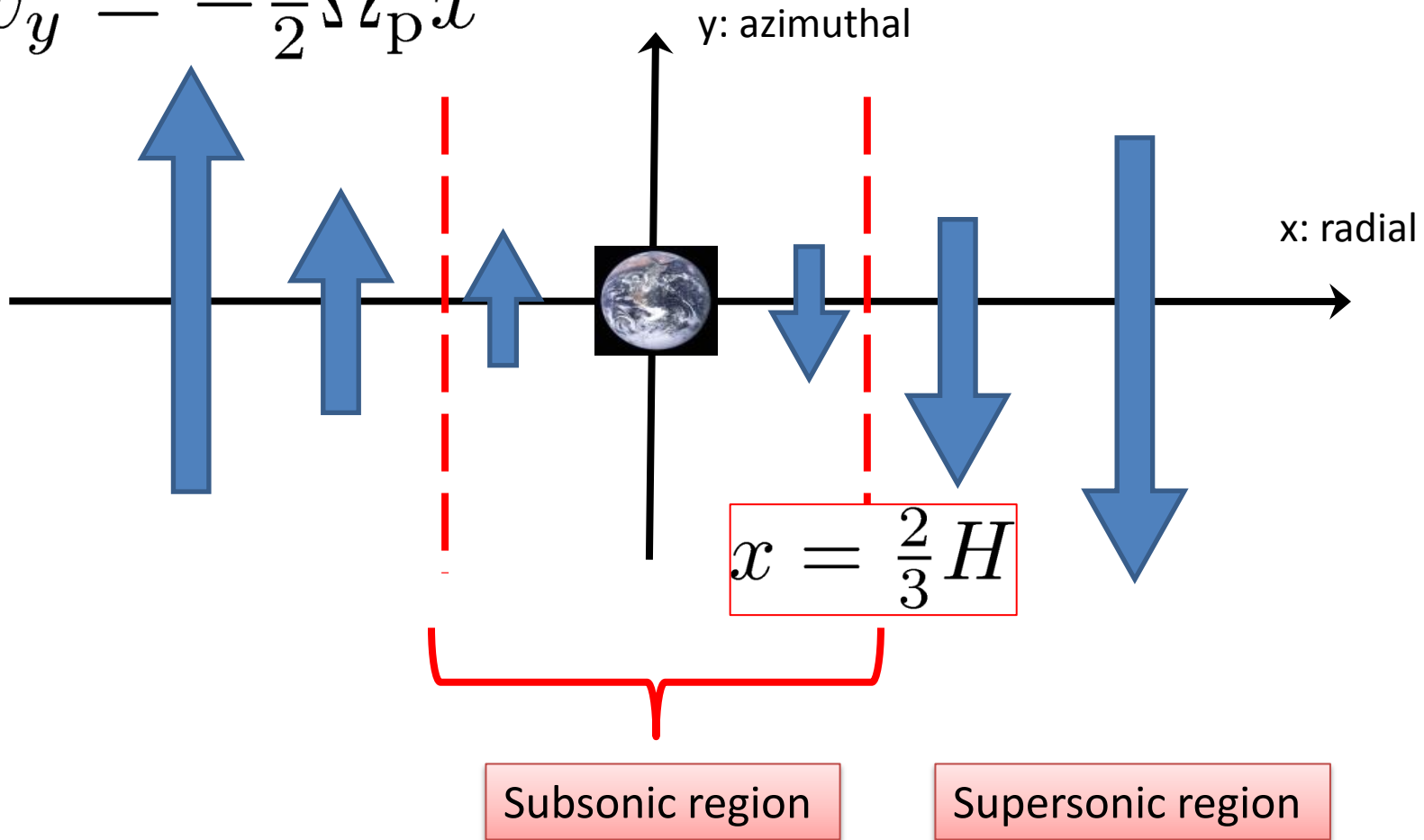
# Surface Density Perturbation



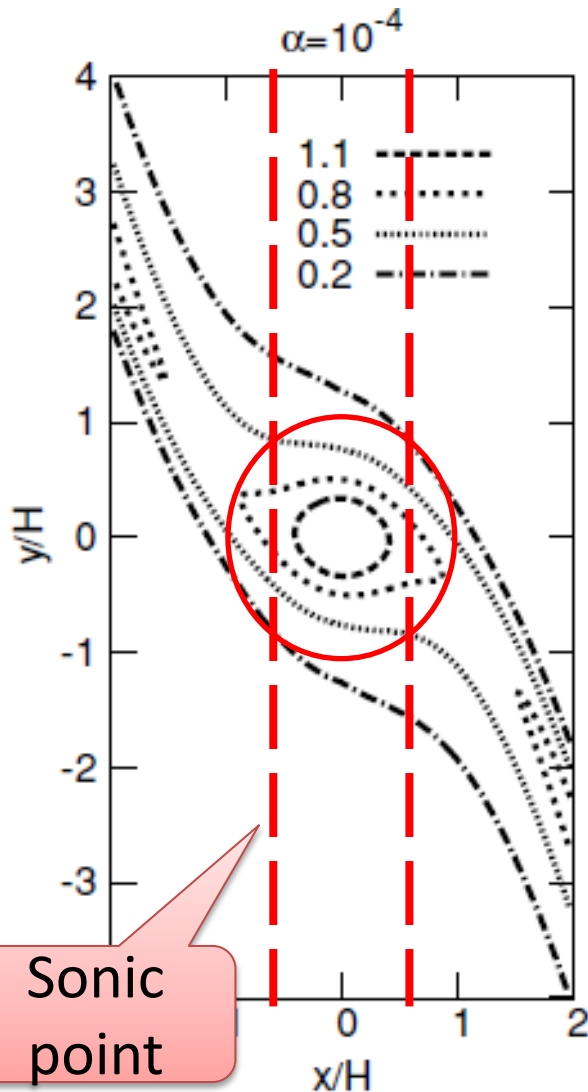
- Spherical structure around the planet
- Spiral density wave launched a little far away from the planet

# Background Velocity Field

$$v_y = -\frac{3}{2}\Omega_p x$$



# Response of Gas in Subsonic Region



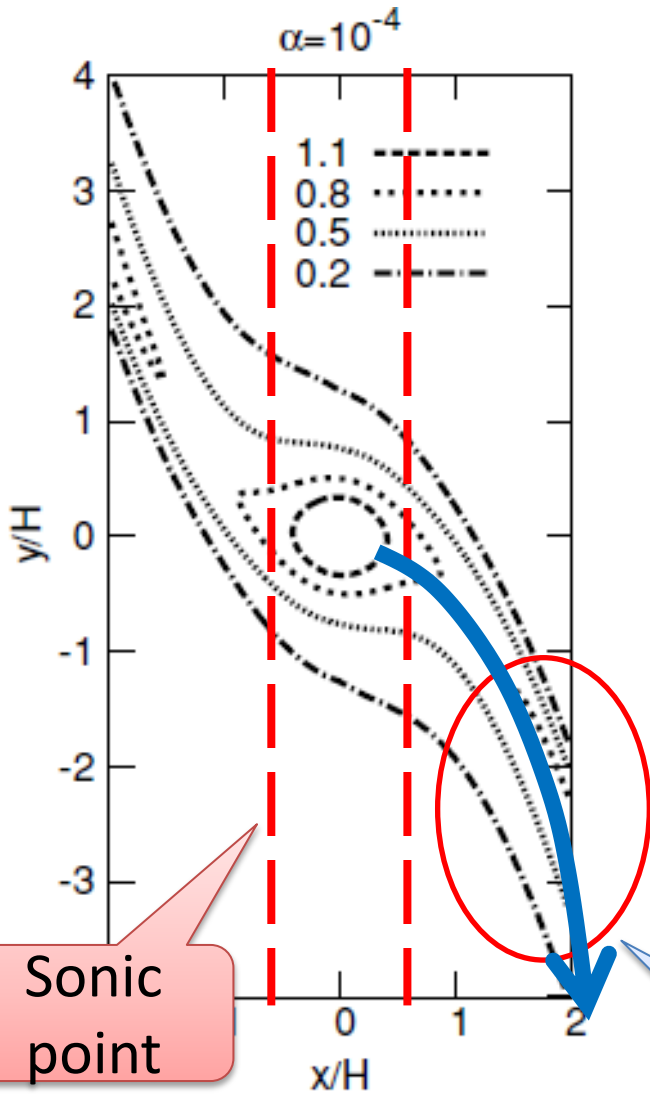
- Hydrostatic equilibrium
- A little tilted due to shear, viscosity...

$$\frac{GM_p}{d} \sim c^2 \frac{\delta \Sigma}{\Sigma}$$

Planet's  
gravitational energy  
d: distance to the  
planet

Gas thermal  
energy  
perturbation

# Response of Gas in Supersonic Region



- Density perturbation  
“carried away” by shear

Characteristic curve (steady state in a supersonic flow):

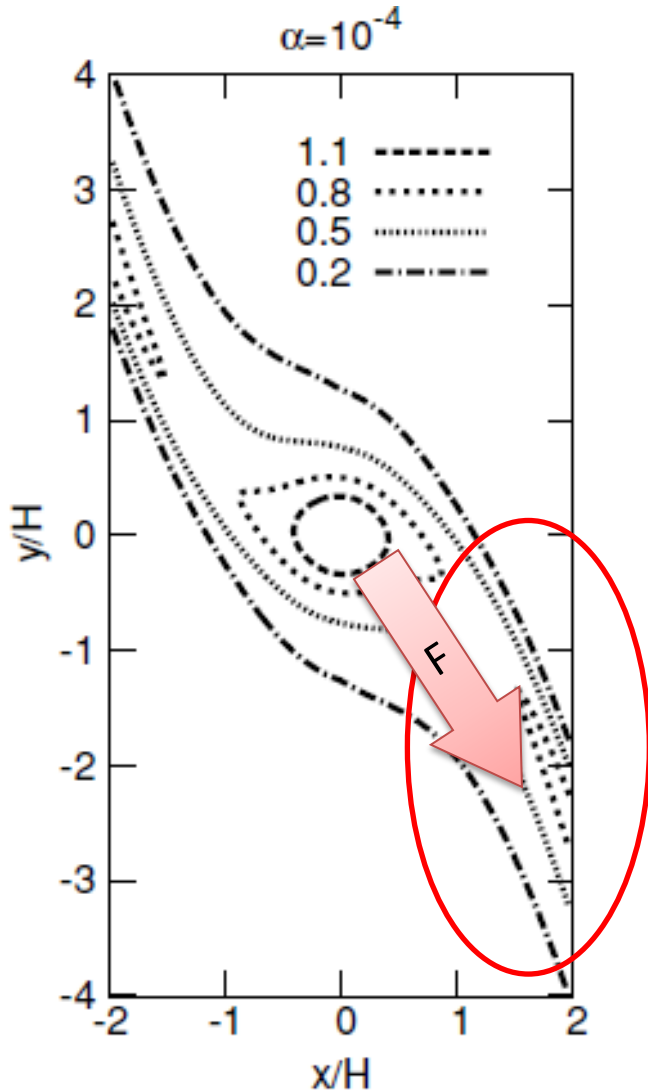
$$\left( \frac{dy}{dx} \right)_{\pm} = \frac{v_x v_y \pm c \sqrt{v^2 - c^2}}{v_x^2 - c^2}$$

Landau & Lishitz

Gives the shape of the spiral:

$$y \sim -\frac{3x^2}{4H} + y_0$$

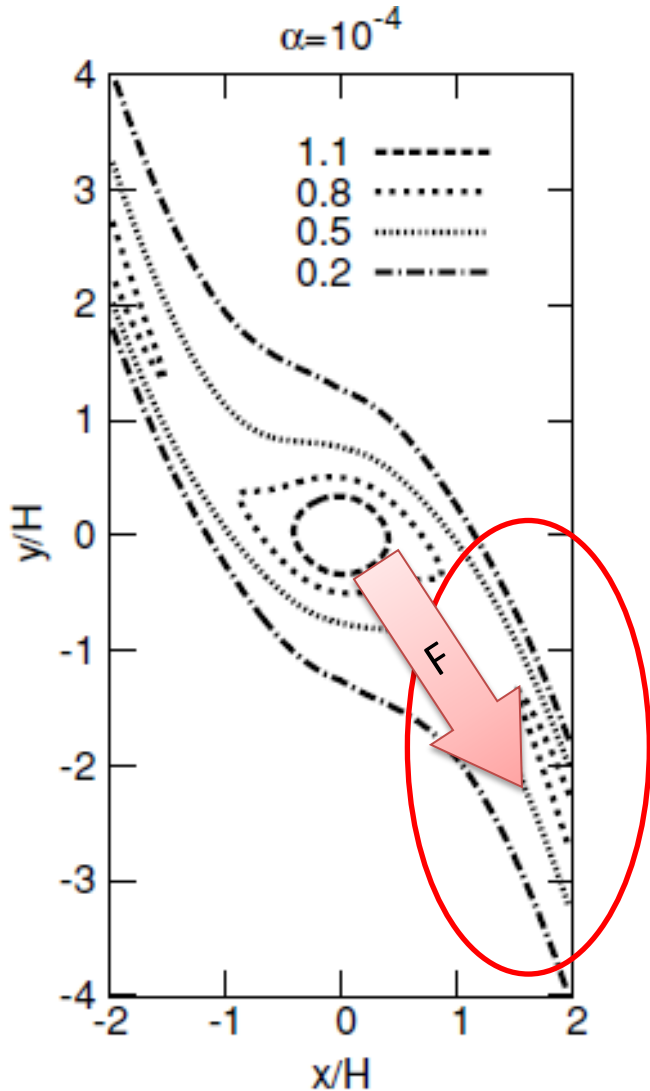
# Backreaction onto the Planet



- Type I migration
- Perturbed surface density exerts gravitational force to the planet



# Order-of-Magnitude of type I rate (1)

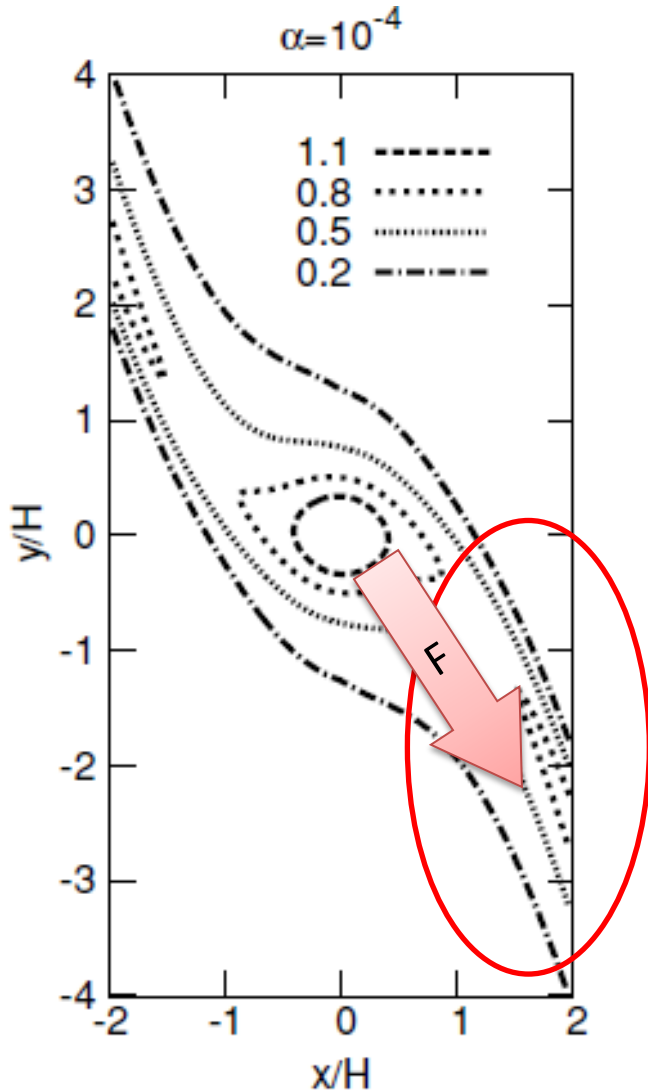


Significant asymmetry in the  $y$ -direction at the sonic point:  
distance  $\sim H$  away from the planet

$$\frac{GM_p}{H} \sim c^2 \frac{\delta \Sigma}{\Sigma}$$

Gives you the estimate of  
surface density perturbation

# Order-of-Magnitude of type I rate (2)



Calculate force from the surface density perturbation

$$F \sim \frac{GM_p(\delta\Sigma H^2)}{H^2}$$

NOTE: this force is from one side of the planet

Differential Force:

$$F \sim \frac{GM_p(\delta\Sigma H^2)}{H^2} \times \frac{H}{r}$$

# Order-of-Magnitude of type I rate (3)

Now you know the force, you can calculate the torque and migration rate

$$T \sim r_p F \sim \frac{dL}{dt} \sim M_p r_p \Omega_p \frac{dr_p}{dt}$$

Migration rate is then given by:

$$\frac{1}{r_p} \frac{dr_p}{dt} \sim \left( \frac{M_p}{M_*} \right) \left( \frac{\Sigma r_p^2}{M_*} \right) \left( \frac{r_p}{H} \right)^2 \Omega_p$$

Typically,  $10^5$  yrs for  $10M_E$  at 5AU  
Much shorter than disk lifetime!

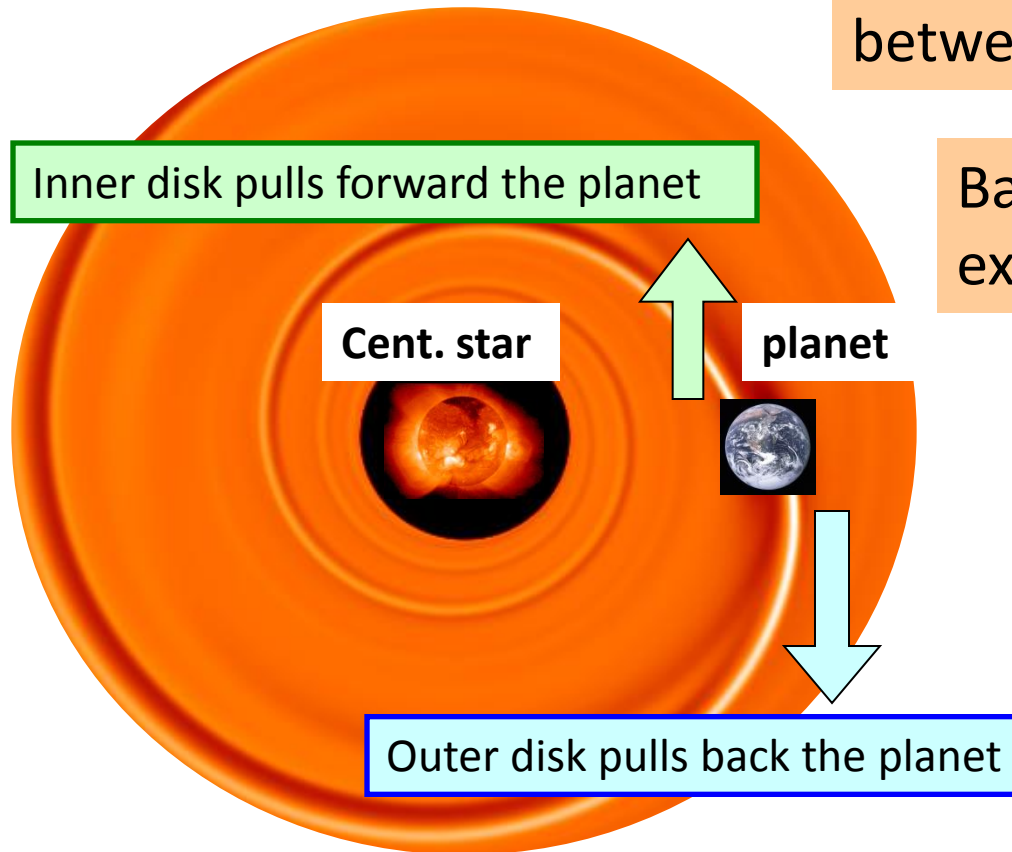
# Disk-Planet Interaction: Brief Summary

Spiral density wave formation due to *gravitational interaction* between the disk and the planet

Back reaction of the wave exerts torque on the planet

After some complicated calculations...

*Protoplanets seems to fall into the central star*



# Some Recent Studies on Migration

- Modification to migration rate and direction due to various physical processes in the disk
  - Viscosity
    - Masset (2001, 2002), Paardekooper and Papaloizou (2009), Muto and Inutsuka (2009)...
  - Self-gravity
    - Baruteau and Masset (2008)...
  - Thermal physics
    - Paardekooper and Mellema (2006), Baruteau and Masset (2008), Paardekooper and Papaloizou (2008), Kley and Crida (2008), Bitsch and Kley (2010), Paardekooper et al. (2010)...
  - Turbulence
    - Nelson and Papaloizou (2004), Oishi et al. (2007), Baruteau and Lin (2010), Baruteau et al. (2011)...
  - Ordered (stable) magnetic field
    - Terquem (2003), Fromang et al. (2005), Muto et al. (2008)...
  - Planet Eccentricity and Inclination
    - Papaloizou and Larwood (2000), Tanaka and Ward (2004), Cresswell and Nelson (2006), Cresswell et al. (2007), Bitsch and Kley (2010), Muto et al. (2011), Rein (2011)...

- Introduction: Planet Formation and Disk-Planet Interaction
- Spiral Density Wave Theory and Type I Planet Migration
- **Direct Imaging Observations of Disk Non-axisymmetric Structures**

# Disk Observation Overview

optically thick at NIR  
optically thin at radio

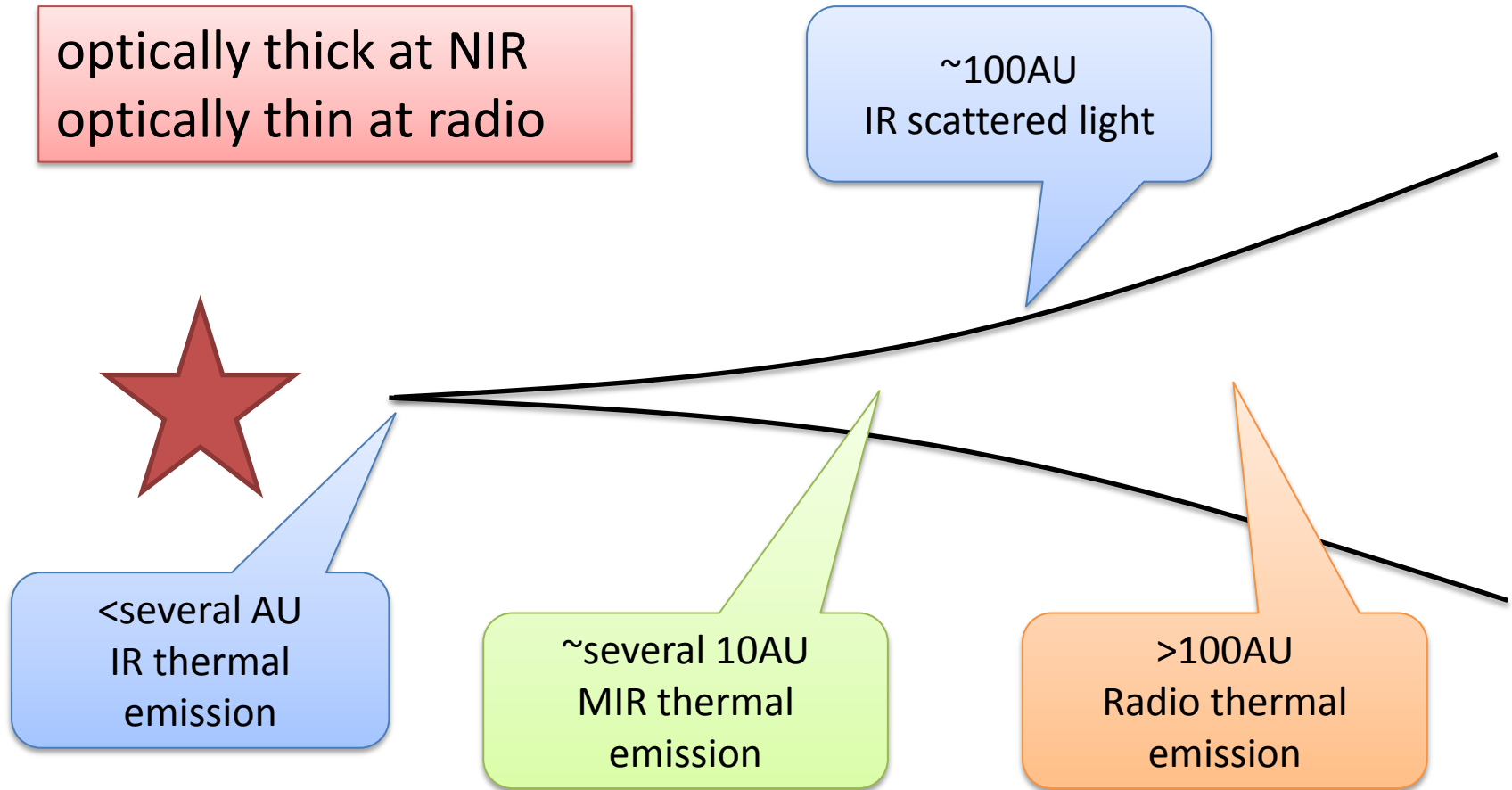
~100AU  
IR scattered light



<several AU  
IR thermal  
emission

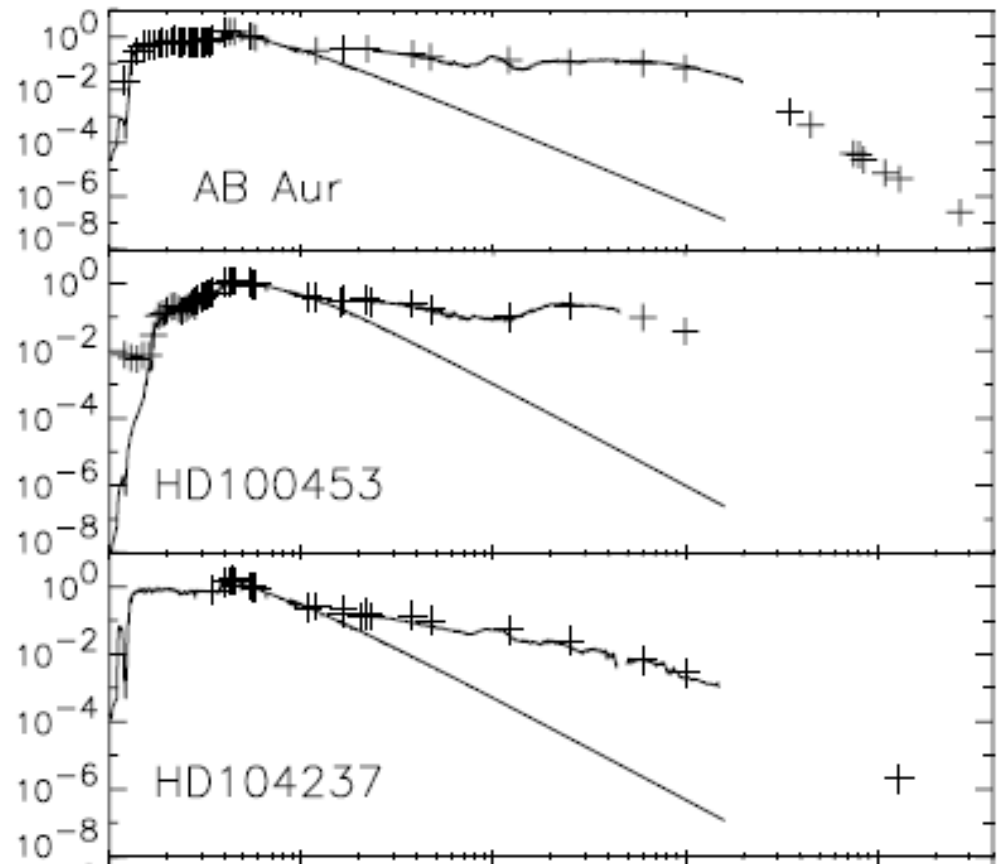
~several 10AU  
MIR thermal  
emission

>100AU  
Radio thermal  
emission



# SED

- Stellar blackbody + excess and longer wavelengths
  - Excess from disk emission
- SED tells us:
  - The existence of the disk
  - The overall structure of the disk



Need to go beyond SEDs if one wants to know more...

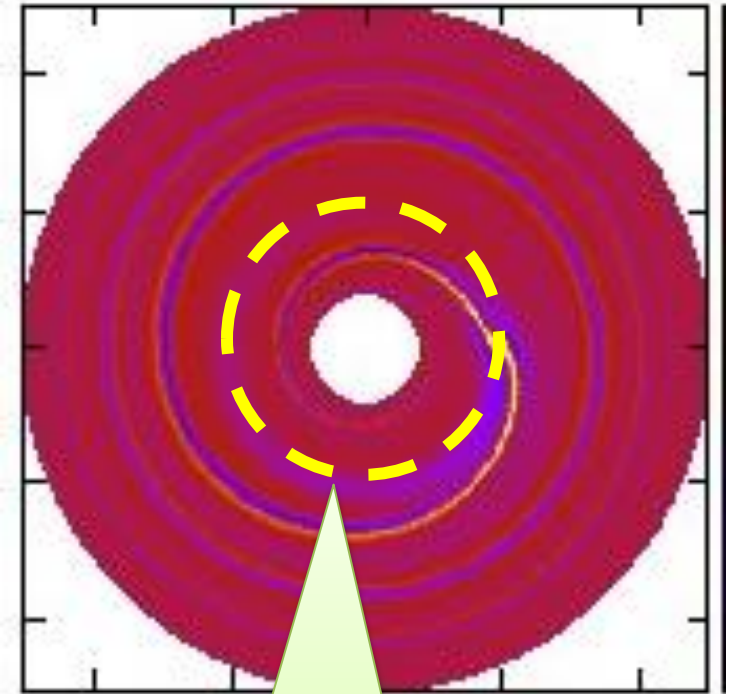


# Detectability of Spiral Structures

- **Spirals are the direct tracer of the dynamical activities in the disk**
- Spirals are just the perturbation to the background disk
  - The overall disk structure is not affected
  - Difficult to find “spirals” in SED
- We need good spatial resolution
  - Spirals are “tightly-wound”
  - Need to distinguish spirals from a ring

# Spiral Density Wave

- Density wave
  - Is a **sound wave** in a differentially rotating disk
  - **Looks stationary** if we are in a **corotating frame**, which *rigidly rotates* at the rotation frequency of the corotation radius
  - Is excited by any perturbation in a disk: turbulence, a planet...



Corotation radius

$$r=r_c$$

# Spiral Shape Detectability: Spatial Resolution

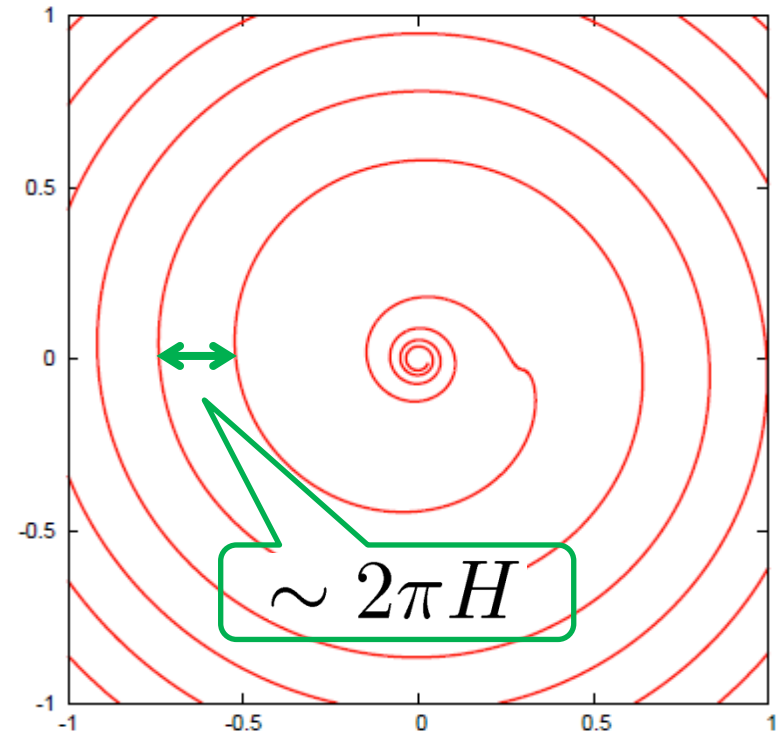
$$\phi(r) \sim \pm \frac{r}{H}$$

Need to resolve  
structure with scale  $\sim H$

$$d = 140 \text{pc}$$

$$R = 100 \text{AU}, H \sim 10 \text{AU}$$

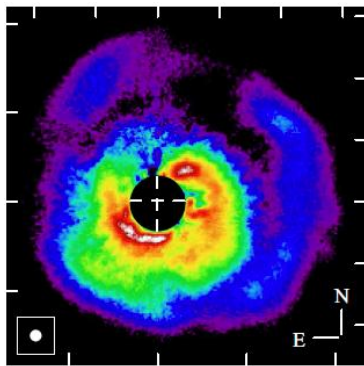
Need  $\sim 0.1 \text{sec}$  resolution  
→ Subaru, ALMA...



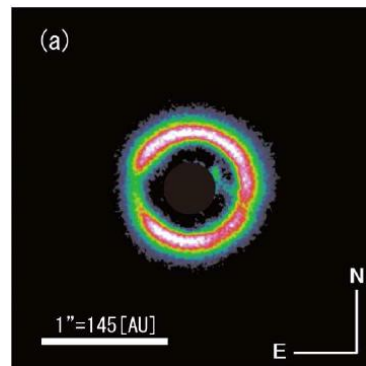
# Strategic Exploration of Exoplanets and Disks with Subaru/HiCIAO



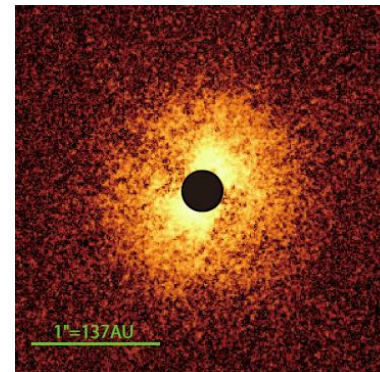
- Direct imaging observations of planets and disks using HiCIAO/AO188 mounted on Subaru
- 120 nights/5years
- Disk observations see polarized light that originates exclusively in the disk



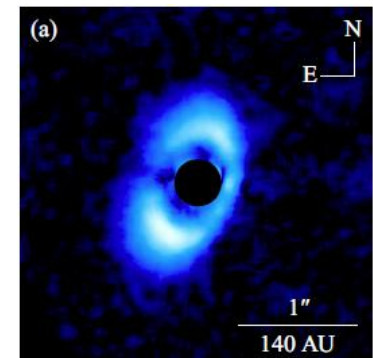
Hashimoto et al.  
2011



Mayama et al.  
2012



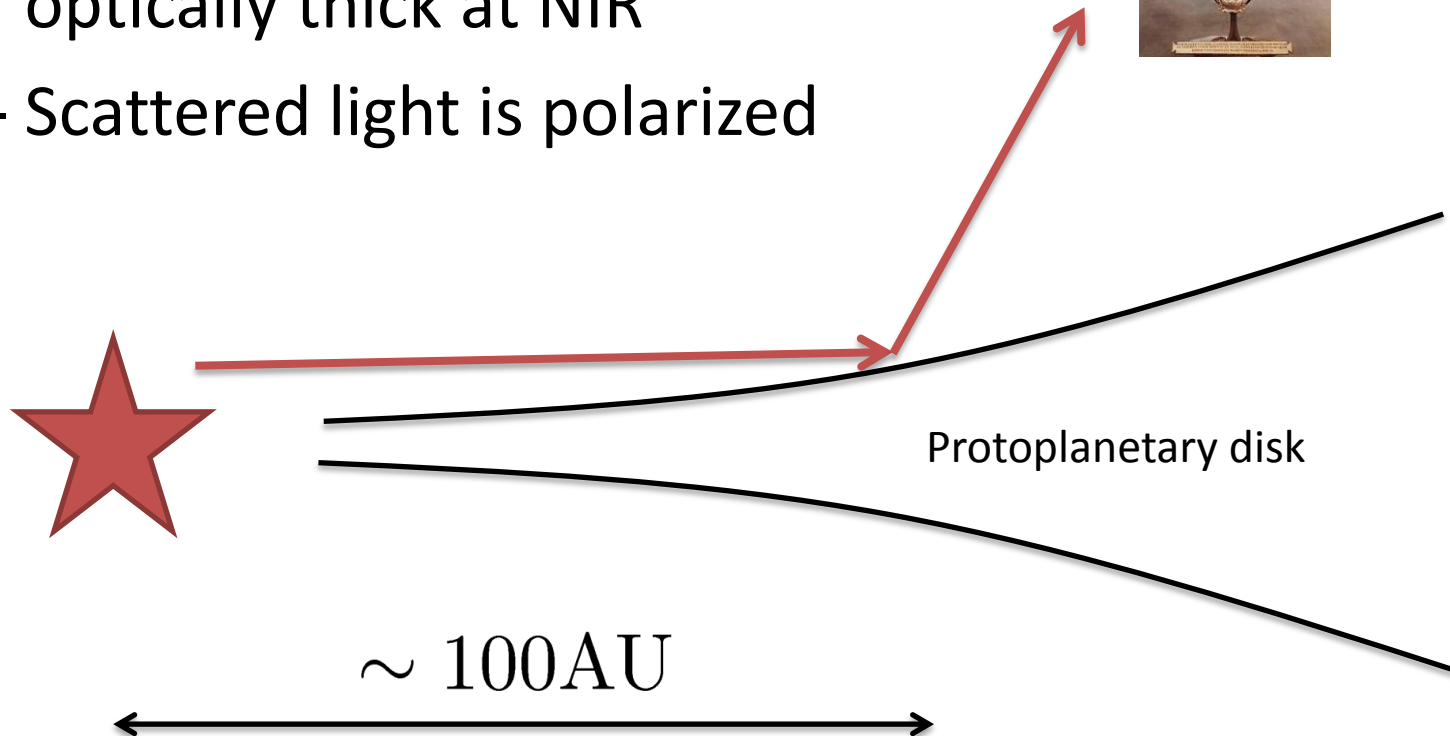
Kusakabe et al.  
2012



Hashimoto et al.  
2012

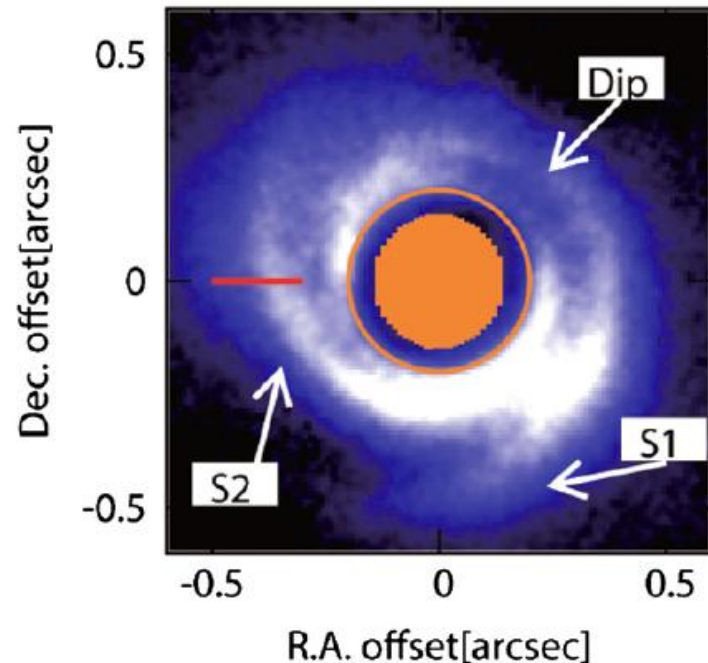
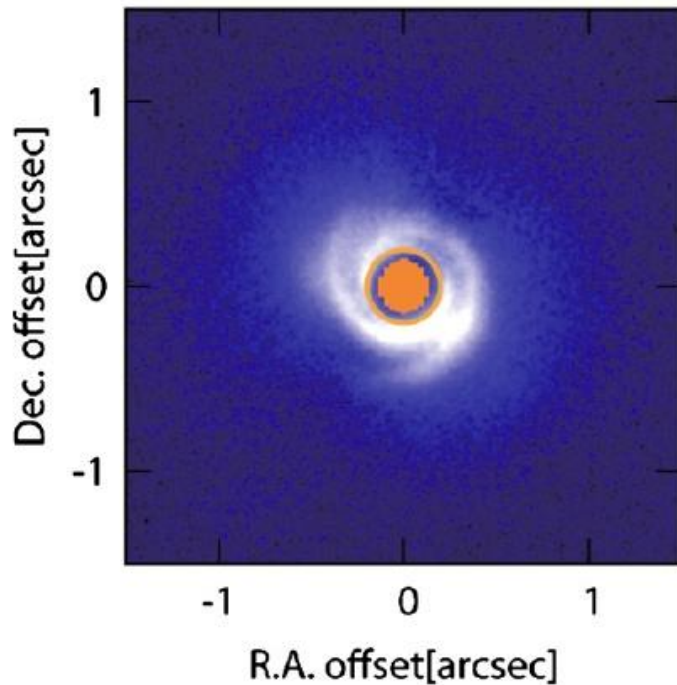
# Direct observation of disks at NIR

- The scattered light from the disk surface is observed
  - Protoplanetary disks are optically thick at NIR
  - Scattered light is polarized

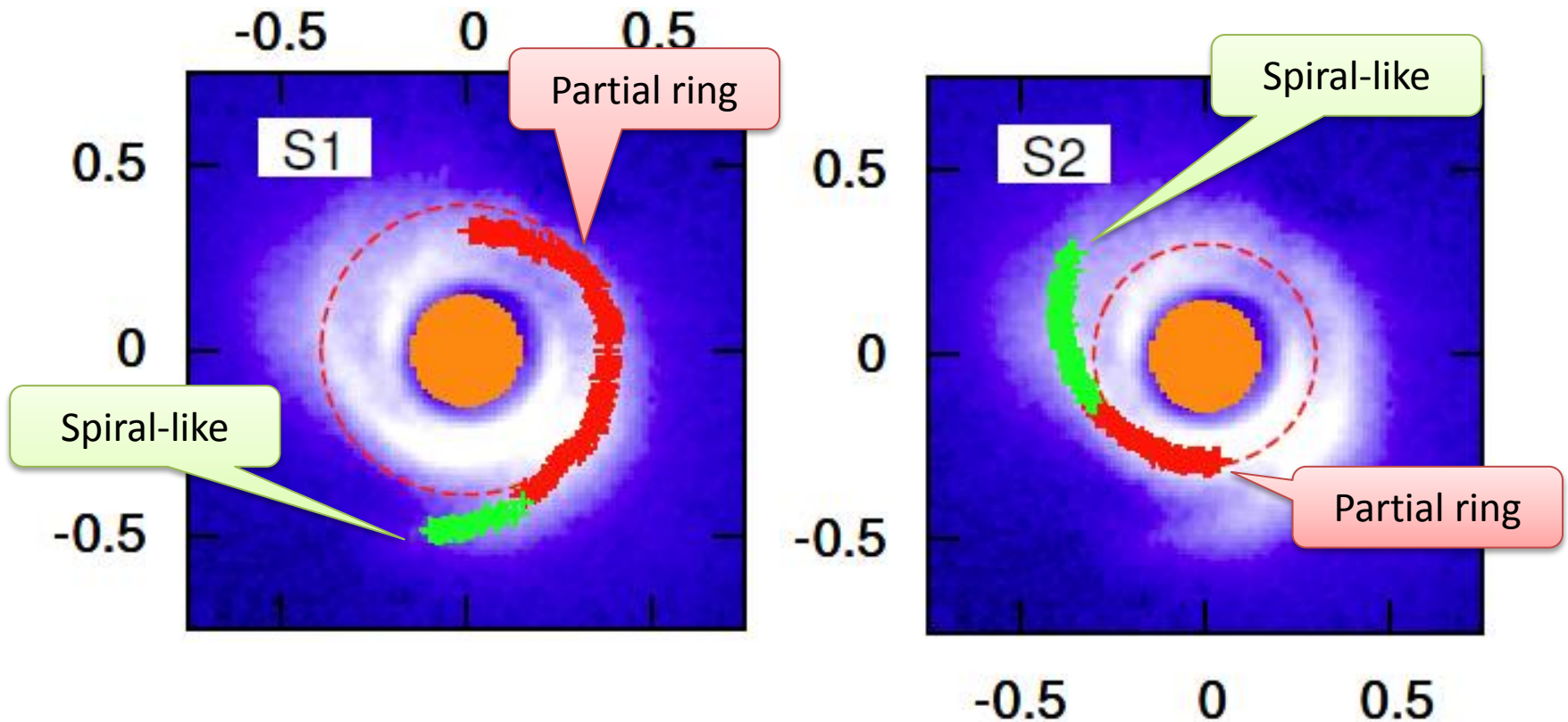


# HD 135344B/SAO 206462 Image

- $\sim 1.7M_{\text{sun}}$  star at  $d \sim 140\text{pc}$
- Polarized intensity image at H-band
- Scattered light is detected even at the “cavity” zone
- Small-scale spiral structure is clearly visible



# Non-Axisymmetric Structures



Density wave theory is used to fit the spiral-like structure

# Model using Density Wave Theory

Spiral shape by density wave theory

$$\theta(r) = \theta_0 - \frac{\text{sgn}(r - r_c)}{h_c} \times \left[ \left( \frac{r}{r_c} \right)^{1+\beta} \left\{ \frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \left( \frac{r}{r_c} \right)^{-\alpha} \right\} - \left( \frac{1}{1+\beta} - \frac{1}{1-\alpha+\beta} \right) \right]$$

Fixed (Kepler)

Disk parameters:

$$\Omega(r) \propto r^{-\alpha}$$

$$c(r) \propto r^{-\beta}$$

Disk thickness  
(temperature)

$$h_c = \frac{H(r_c)}{r_c}$$

Fixed (almost const.  
opening-angle)

Parameters for spiral location:

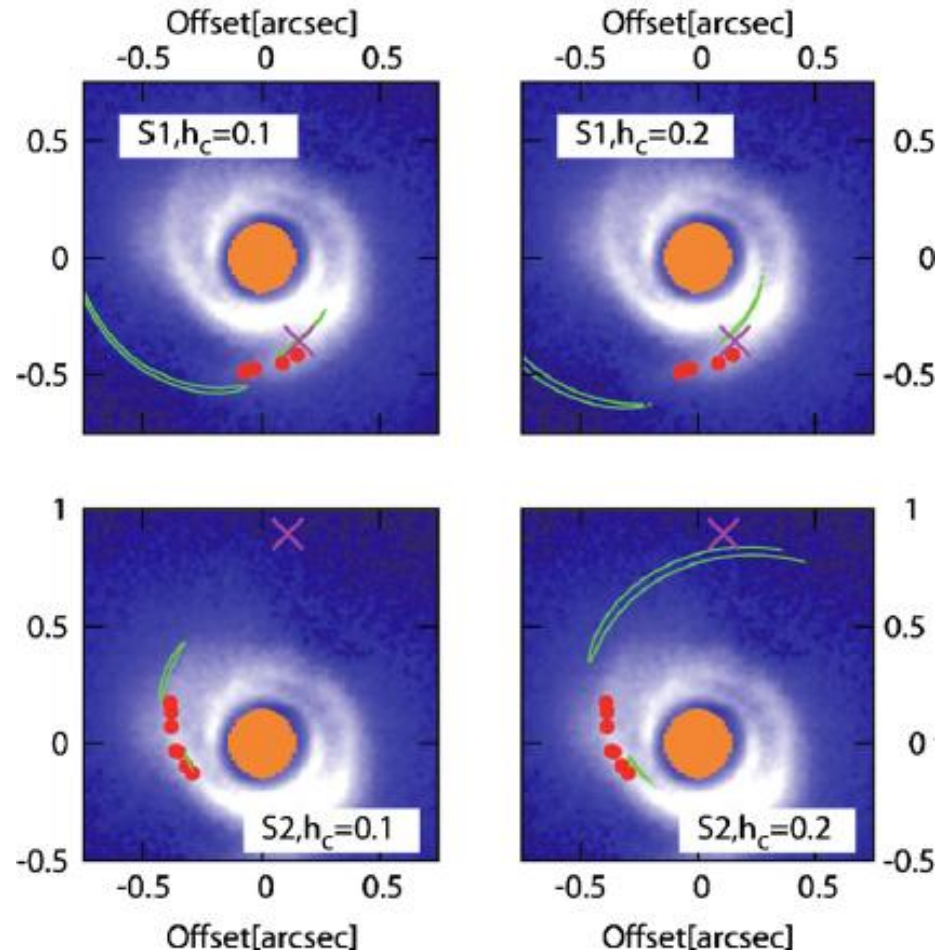
$r_c$  : corotation radius

$\theta_0$  : azimuthal phase



# Fitting Results

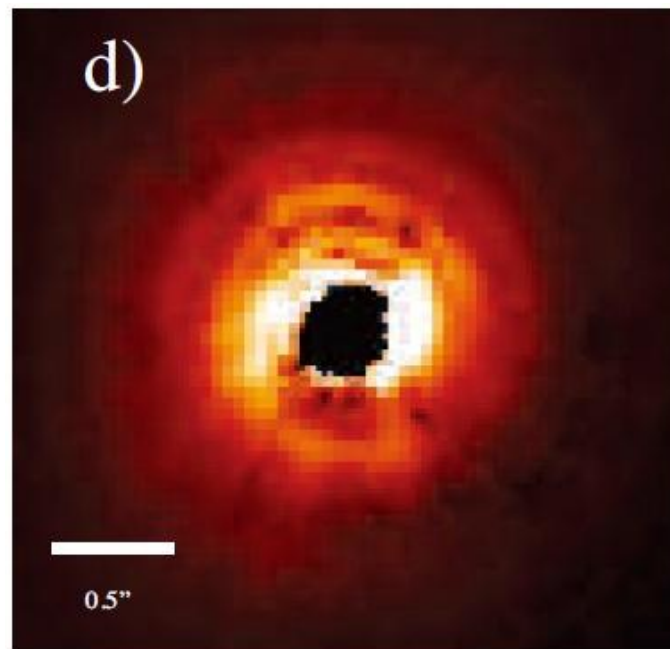
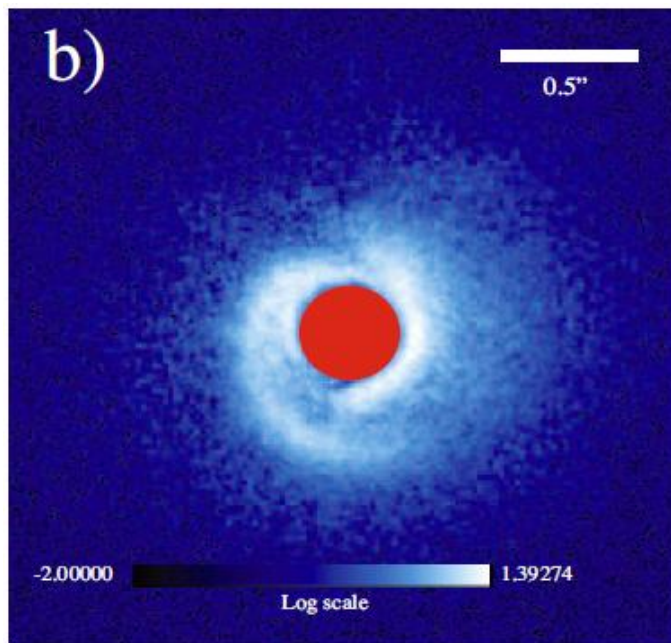
- Significant parameter degeneracy, but...
  - $H/R \sim 0.1-0.2$  is consistent with the spiral structure
  - Also consistent with sub-mm estimate
- Prediction for the “launching point” of the spiral
  - Prediction for the corotation radius
  - Prediction for the **time evolution of the spiral structure**



$$\Omega_{\text{pattern}} = 0.8 \left( \frac{r_c}{70\text{AU}} \right)^{-3/2} \left( \frac{M_*}{1.7M_{\odot}} \right)^{1/2} \text{ [deg/yr]}$$

# MWC 758/HD 36112 Image

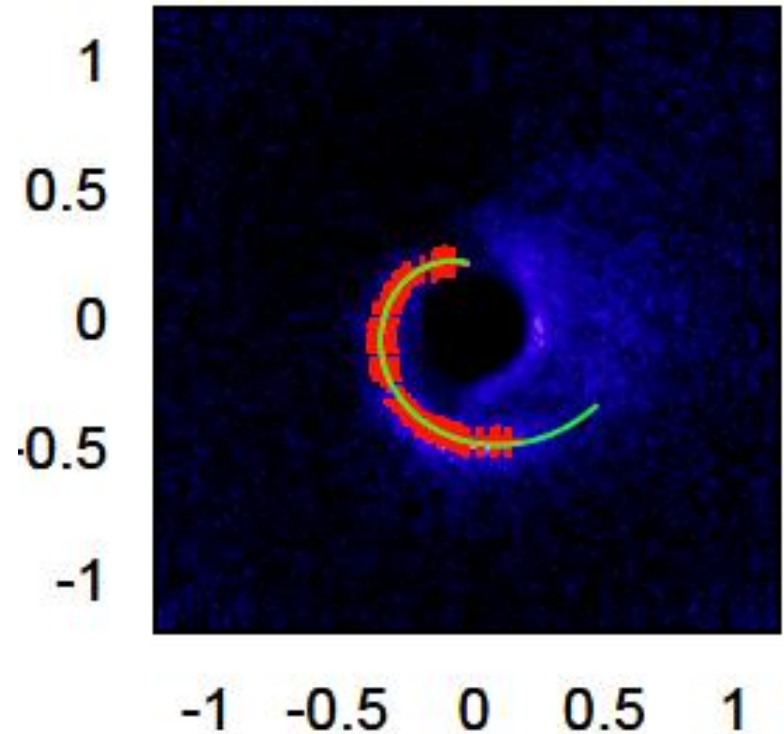
- $\sim 2M_{\text{sun}}$  star at  $d \sim 200\text{-}300\text{pc}$
- Polarized intensity image at H-band, Intensity at K-band
- (A) spiral structure(s) is/are visible in both bands



# Spiral fitting for MWC 758

Parameter	Search Range	Best Fit External Perturber
$r_c$	$0''.05 \leq r_c \leq 1''.55$	$r_c = 1''.55$
$\theta$	$0 \leq \theta_0 \leq 2\pi$	$\theta_0 = 1.72[\text{rad}]^a$
$h_c$	$0.05 \leq h_c \leq 0.25$	$h_c = 0.182$
$\delta$	$-0.1 \leq \delta \leq 0.6$	$\delta = 0.06$

- Corotation radius is likely at outer radii
  - $R_c \sim 1.55 \text{asec}$
- Rather hot ( $\sim$  thick) disk
  - $H/R \sim 0.18$

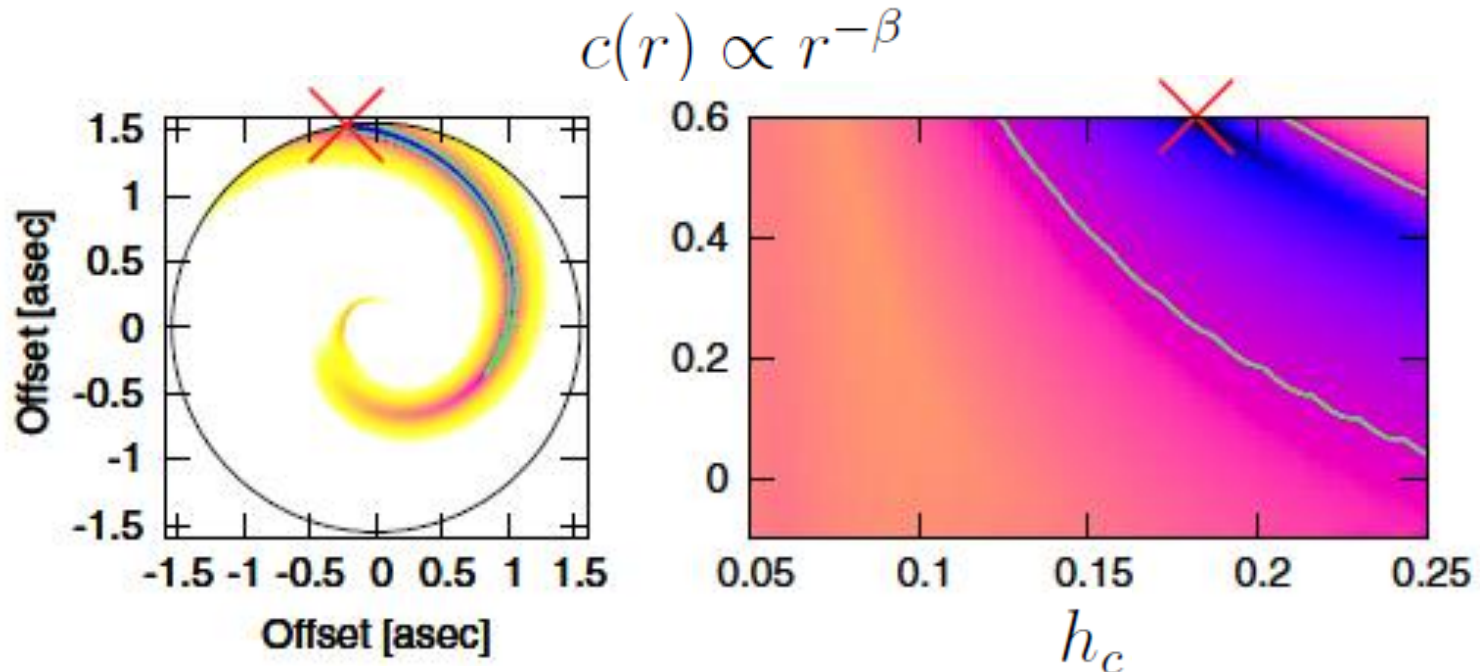


# Parameter Degeneracy

Launching point

Sound velocity distribution

パラメータ:  $(r_c, \theta_0, h_c, \alpha, \beta)$



- Corotation at outer radii?
- $H/R > 0.1$ , the disk can be both flat or flared

# What is the Origin of the Spiral?

I don't know.

But let's assume it is a planet, then:

$$\frac{\delta\Sigma}{\Sigma} \sim \frac{M_p}{M_*} \left( \frac{r}{H} \right)^3$$

This yields:

- ~0.5 Jupiter Mass for SAO 206462
- ~5 Jupiter Mass for MWC 758

and its location can be predicted by the spiral fitting

Disk structure as a probe of *indirect signature* of an embedded planet (signposts of planets)

I DON'T KNOW WHO  
THIS IS



BUT MY FRIENDS  
SAY HIES COOL.

# Summary

- Disk-planet interaction is one of important dynamical processes in protoplanetary disks
- Disk-Planet interaction:
  - Excites spiral waves and opens up a gap
  - Causes radial migration of a planet
- It is now possible to observe spiral structures in the disk with Subaru
  - A relatively simple model for spirals is given
- ALMA will definitely reveal spiral structures in the near future

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