

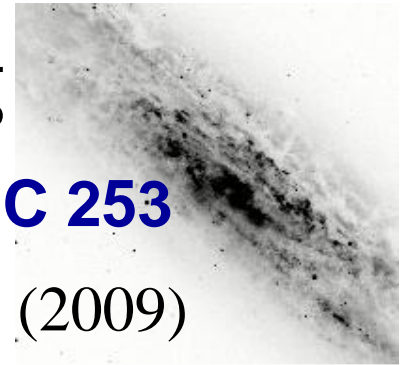
*Shattering and Coagulation of Dust  
Grains in Interstellar Turbulence*

**Hiroiyuki Hirashita (平下 博之)**  
(ASIAA, Taiwan)

# *Outline*

1. Dynamical Grain-Gas Coupling
2. Interstellar Turbulence
3. Formulation of Shattering and Coagulation
4. In a Cosmological Context

# 1. Dynamical Grain-Gas Coupling

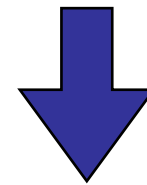


**NGC 253**

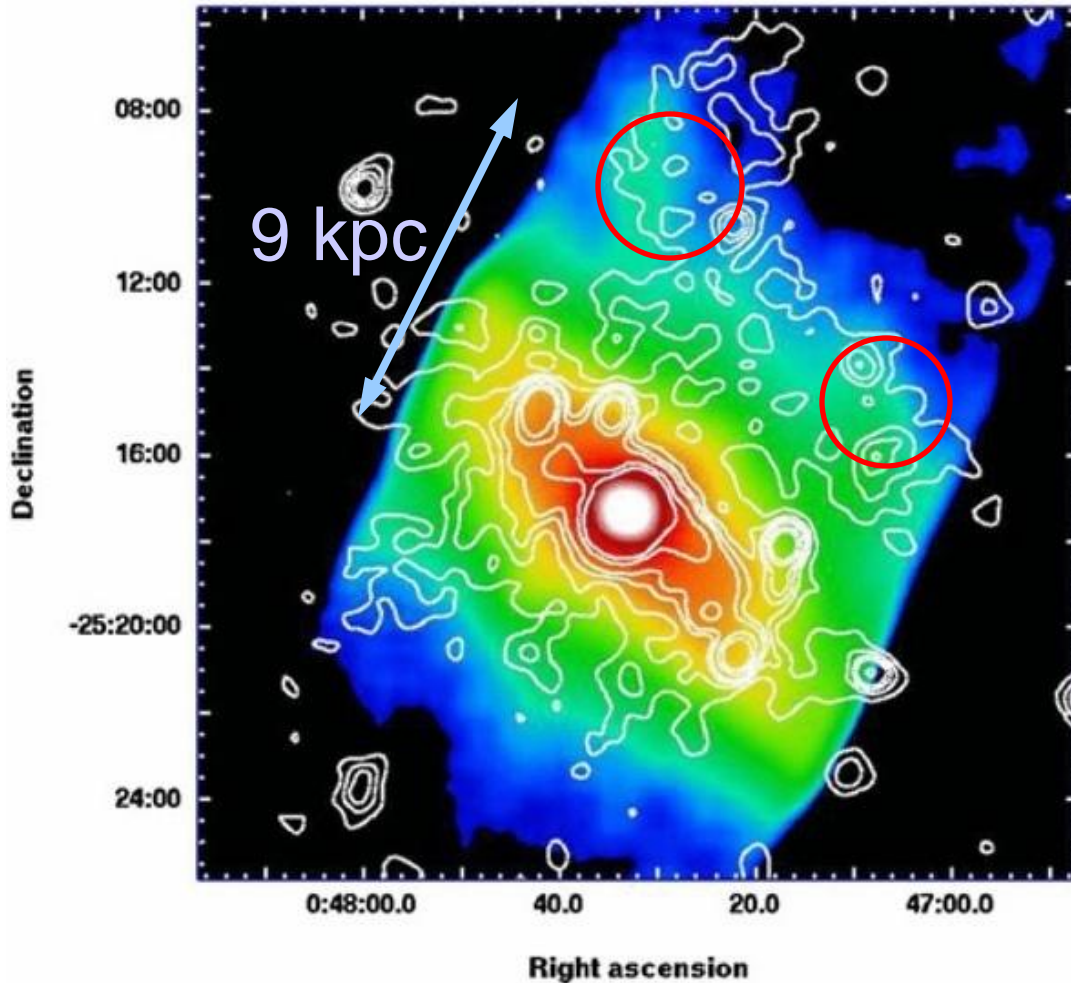
Kaneda et al. (2009)

color: *AKARI* 90  $\mu\text{m}$   
contour: *ROSAT* X-ray

The FIR extension  
coincides with the X-  
ray structure.

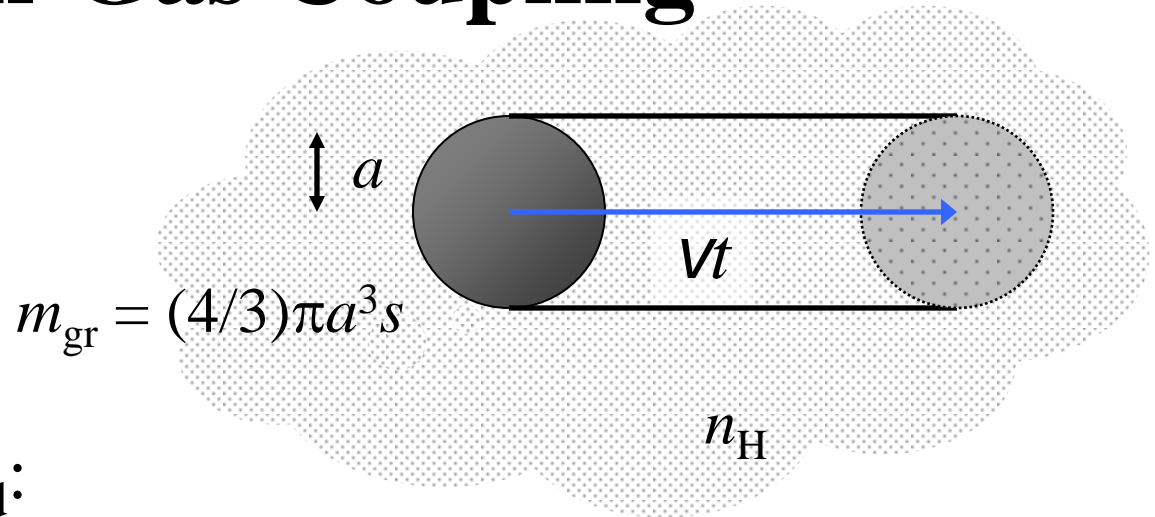


Dust is transported by  
gas ejection induced  
by stellar activity.



$$V_{\text{escape}} = 280 \text{ km/s}$$
$$9 \text{ kpc} / 280 \text{ km/s} = 30 \text{ Myr}$$

# Grain-Gas Coupling



Gas drag timescale  $t_d$ :

$$(m_H v)(\pi a^2 v n_H) t_d \sim m_{\text{gr}} v.$$

Grain motion is coupled with the gas motion on a scale  $l$  large enough:

$$l \sim vt_d = (4/3)as/(m_H n_H) \sim (10/n_H)(a/0.1 \mu\text{m}) \text{ pc}$$

Large grains tend to be coupled with larger motions.

# 2. Interstellar Turbulence

ISM is turbulent (often supersonic)  
(e.g., McKee & Ostriker 2007).

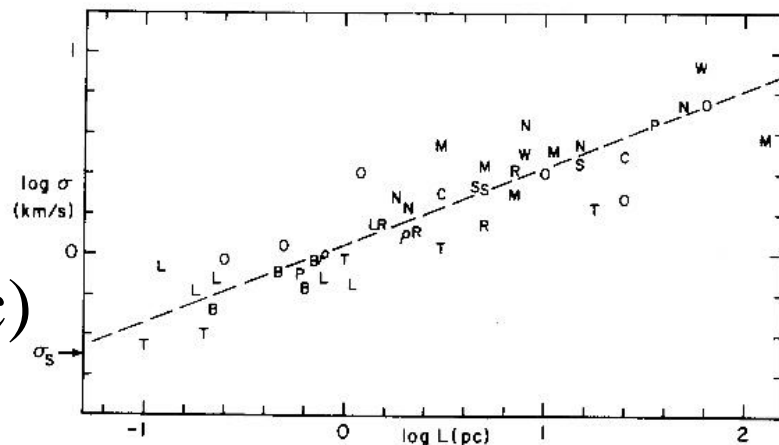
Implication for shattering (disruption):

$c_s \sim 10$  km/s in warm ( $\sim 8000$  K) medium

→ above the shattering threshold ( $\sim$  a few km/s).

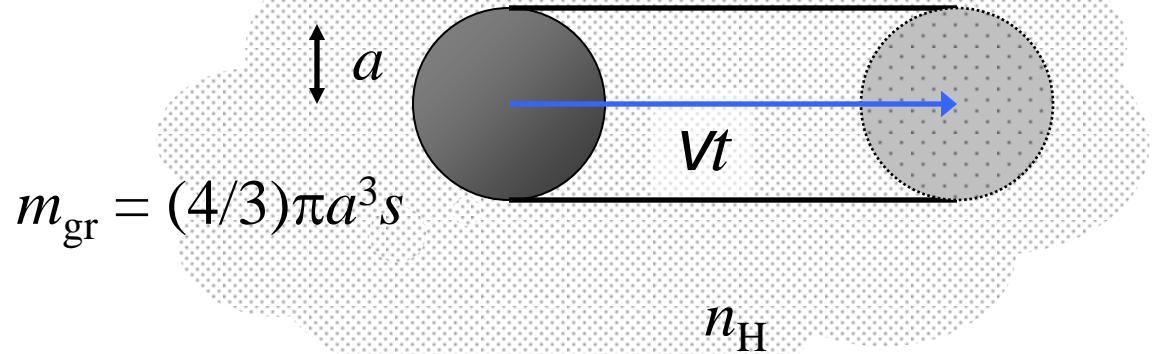
Implication for coagulation (sticking):

$V_{\text{turb}} \gg$  grain thermal speed. → If grain motion is coupled with turbulence, grain-grain collision occurs frequently (e.g., Ossenkopf 1993).



Larson (1981)

# Grain-Turbulence Coupling



Grain motion is coupled with the gas motion on a scale  $l$  large enough:

$$l \sim vt_d = (4/3)as/(m_H n_H) \sim (10/n_H)(a/0.1 \mu\text{m}) \text{ pc}$$

Large grains tend to be coupled with larger motions.

Kolmogorov turbulence:  $v_{\text{turb}} \propto l^{1/3}$

Large grains tend to acquire larger velocities.

# Gyroresonance

Magnetic fields ( $B^2/8\pi \sim nkT$ ) + Grain charge

→ MHD wave + gyro-motion of grains

Resonance between wave and gyro-motion

(gyroresonance):  $\omega - k_{\parallel} v \cos \theta = n\omega_{\text{gyro}}$

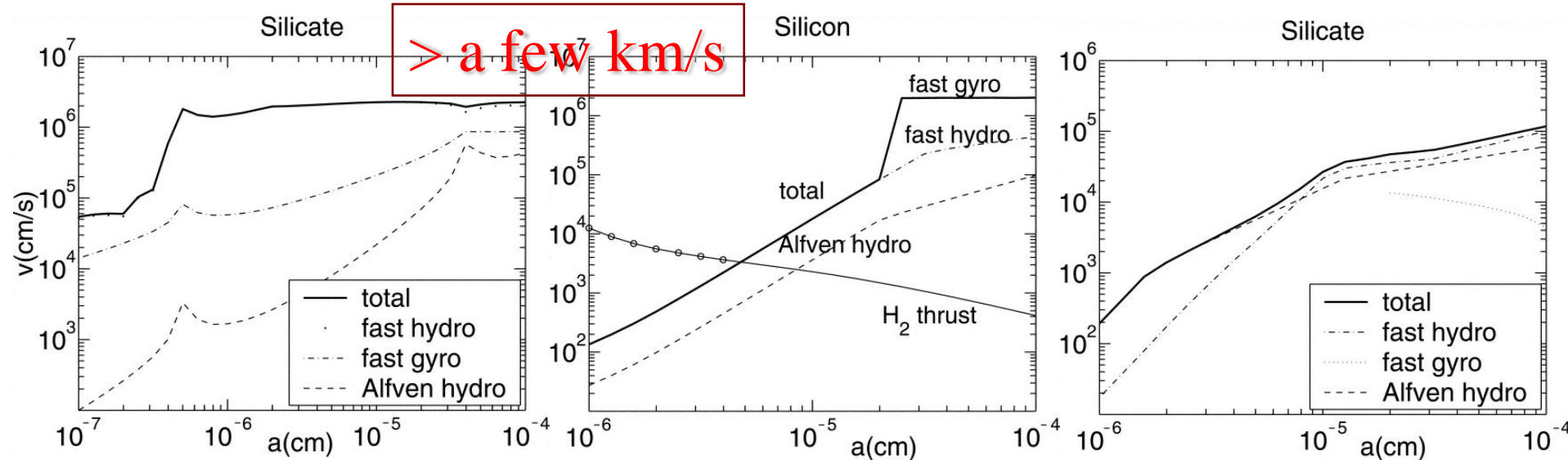
Large grains are further accelerated.

# Grain Velocities

MHD turbulence model

Yan, Lazarian, & Draine (2004)

hydro-drag, gyro-resonance



Warm ionized medium

$$T = 8000 \text{ K}$$

$$n_H = 0.1 \text{ cm}^{-3}$$

$$B = 3.4 \text{ } \mu\text{G}$$

Warm neutral medium

$$T = 6000 \text{ K}$$

$$n_H = 0.3 \text{ cm}^{-3}$$

$$B = 5.8 \text{ } \mu\text{G}$$

Dense cloud

$$T = 10 \text{ K}$$

$$n_H = 10^4 \text{ cm}^{-3}$$

$$B = 80 \text{ } \mu\text{G}$$

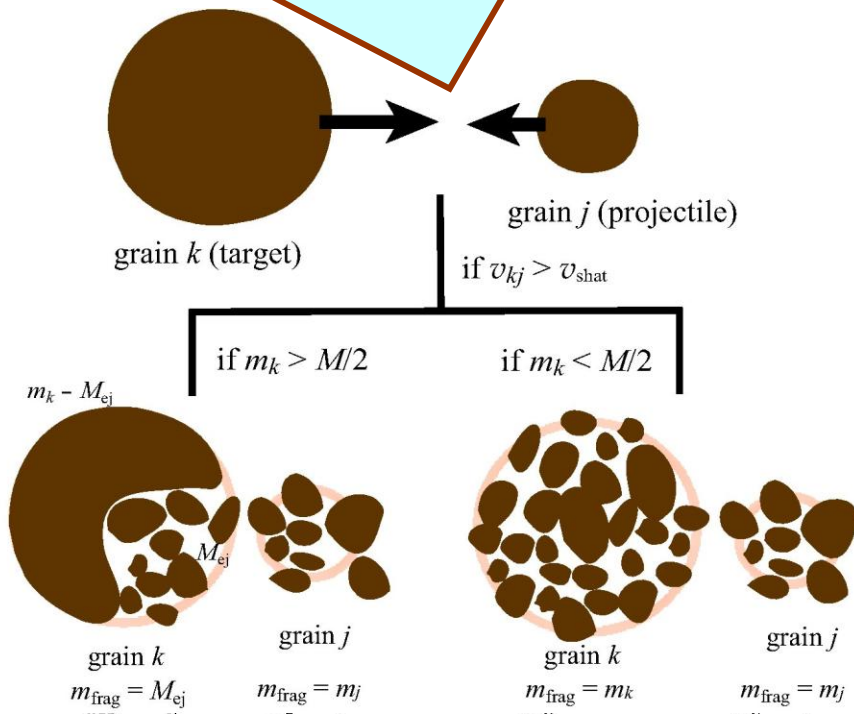


# Coagulation

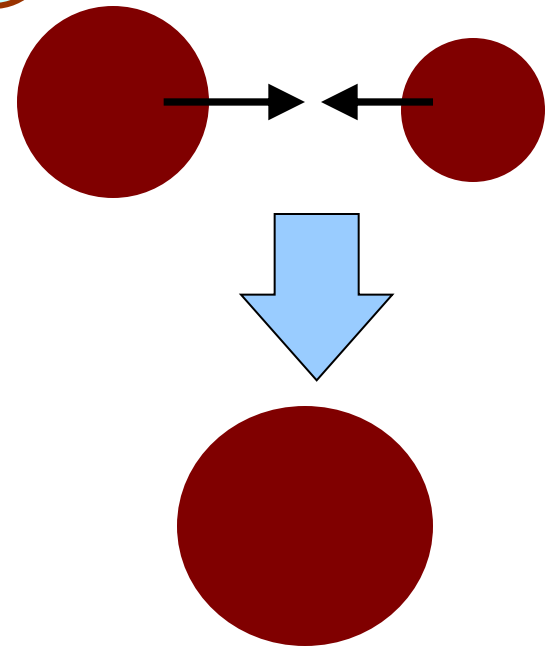
Relative velocities can be excited by interstellar turbulence.

Shattering

Coagulation



Shattering threshold:  
2.7 km/s (silicate), 1.2 km/s (graphite)  
(Jones et al. 1996)



coagulation rate = grain-grain collision rate  
Threshold:  $\sim 10^3$  cm/s

# Grain Size Distribution and Extinction

## Extinction (absorption+scattering)

$$\tau_{\lambda,i} = \int_0^{\infty} \pi a^2 Q_{\lambda}(a) N_{\text{dust}}(a) da$$

$a$ : grain radius ( $\llsim 0.1 \mu\text{m}$ )

$Q_{\lambda}(a) \sim 1$  for  $\lambda \llsim a$

$Q_{\lambda}(a) \ll 1 \propto a$  for  $\lambda \gg a$

$$\tau_{\lambda} = \sum_i \tau_{\lambda,i}$$

$i$ : grain species (silicate, graphite)

Grain size distribution  $N_{\text{dust}}(a) \propto a^{-3.5}$

with  $0.005 \mu\text{m} < a < 0.25 \mu\text{m}$ : MRN

## What determines the grain size distribution?

- ❑ Source (supernova, AGB stars, etc.)
- ❑ **Shattering and coagulation?**

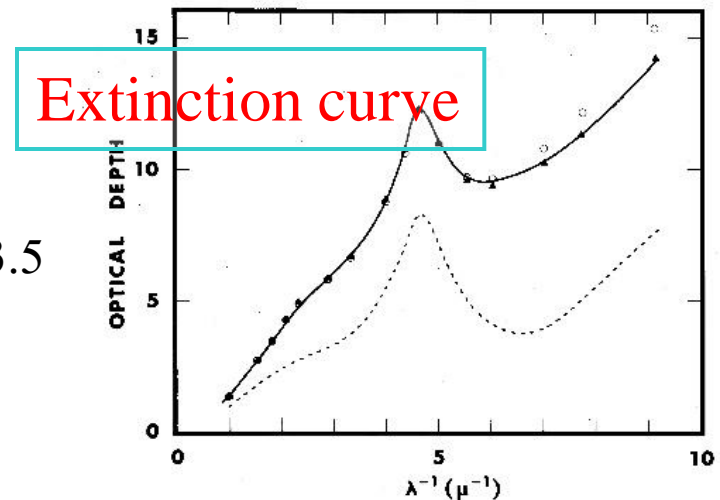
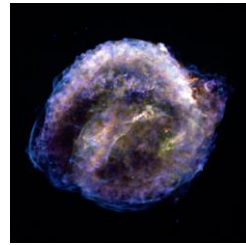


FIG. 4.—Optical depths, for column densities of  $10^{22}$  H atoms  $\text{cm}^{-2}$ , versus inverse wavelength. *Solid line*: observed by OAO. *Triangles*: the extinction of (C + Ol) mixture of Fig. 2. *Dashed line*: the contribution of graphite to the extinction. *Dots*: a mixture of graphite and olivine,  $n(a) \propto a^{-3.6}$ ,  $0.005 \mu\text{m} < a < 0.25 \mu\text{m}$ , forced to fit at the maximum of the “bump” at  $4.6 \mu\text{m}^{-1}$ .

Mathis, Rumpl, &  
Nordsieck (1977)

# ISM Recycling and Dust

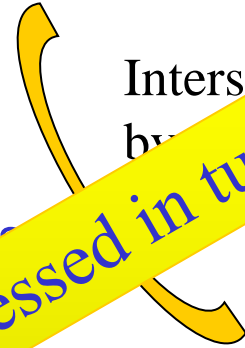
Nuclear reaction



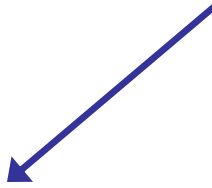
Gas

Metal

Interstellar clouds  
by (wave  
destruction)



Interstellar  
gas



star formation  
(astration)

molecular cloud  
(dust growth)

**Turbulence is ubiquitous. → Grains are processed in turbulence?**

QuickTime®  
TIFF (LZW) 8-bit color image  
© 1999 Apple Computer, Inc. All rights reserved.

# Specific Questions

- A) Evolution of grain size distribution by **shattering and coagulation** under the grain motion induced by *ubiquitous* turbulence.
- B) Do shattering and coagulation have a significant imprint in the **extinction curve**?

# 3. Formulation

Hirashita & Yan (2009)

Discrete size bins  $a_0, \dots, a_N$

The  $i$ -th bin contains grains of  $\tilde{\rho}_i$  [ $\text{g cm}^{-3}$ ].

Shattering

$$\left[ \frac{d\tilde{\rho}_i}{dt} \right]_{\text{shat}} = -m_i \tilde{\rho}_i \sum_{k=1}^N \alpha_{ki} \tilde{\rho}_k + \sum_{j=1}^N \sum_{k=1}^N \alpha_{kj} \tilde{\rho}_k \tilde{\rho}_j m_{\text{shat}}^{kj}(i),$$

$$\alpha_{ki} = \begin{cases} \frac{\sigma_{ki} v_{ki}}{m_i m_k} & \text{if } v_{ki} > v_{\text{shat}}, \\ 0 & \text{otherwise,} \end{cases}$$

distribution of shattered fragments  
(power-law)

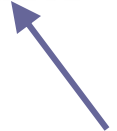


Coagulation

$$\left[ \frac{d\tilde{\rho}_i}{dt} \right]_{\text{coag}} = -m_i \tilde{\rho}_i \sum_{k=1}^N \alpha_{ki} \tilde{\rho}_k + \sum_{j=1}^N \sum_{k=1}^N \alpha_{kj} \tilde{\rho}_k \tilde{\rho}_j m_{\text{coag}}^{kj}(i),$$

$$\alpha_{ki} = \begin{cases} \frac{\sigma_{ki} v_{ki}}{m_i m_k} & \text{if } v_{ki} < v_{\text{coag}}^{ki}, \\ 0 & \text{otherwise.} \end{cases}$$

$m_k + m_j$



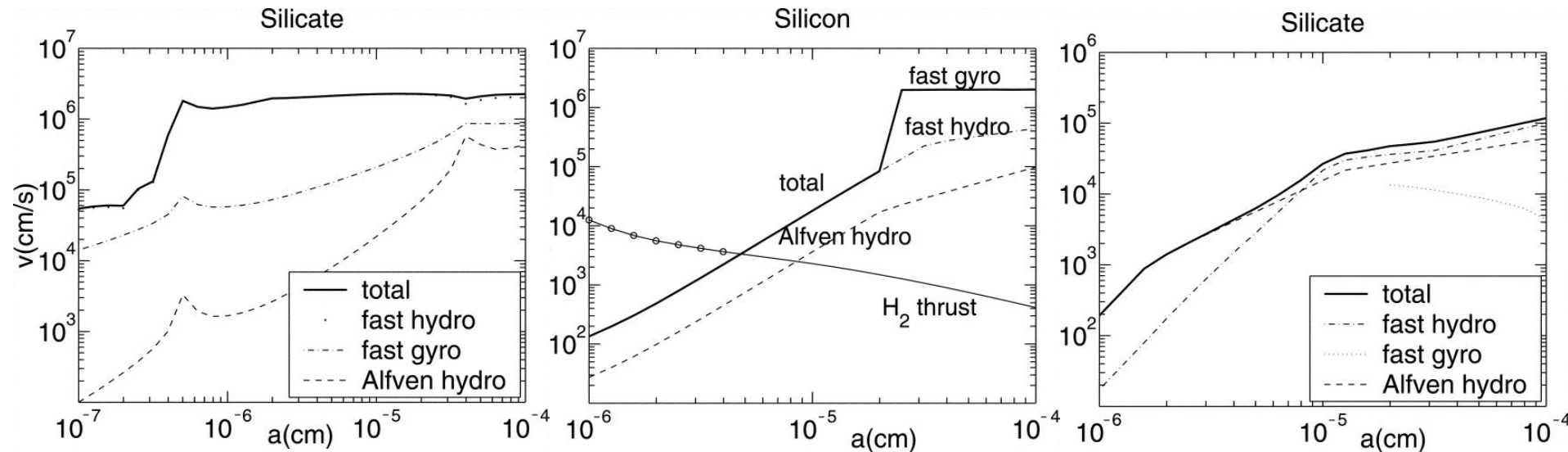
The grain velocities are adopted from Yan et al. (2004) (MHD turbulence).

# Grain Velocities

MHD turbulence model

Yan, Lazarian, & Draine (2004)

hydro-drag, gyro-resonance



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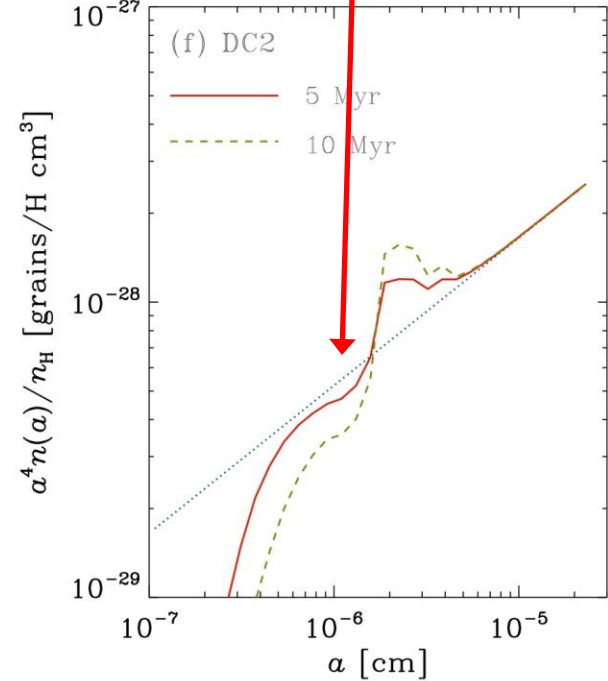
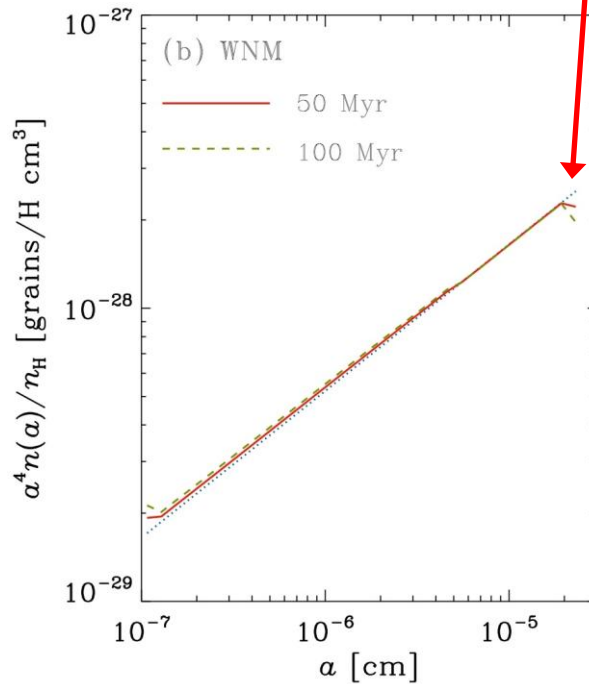
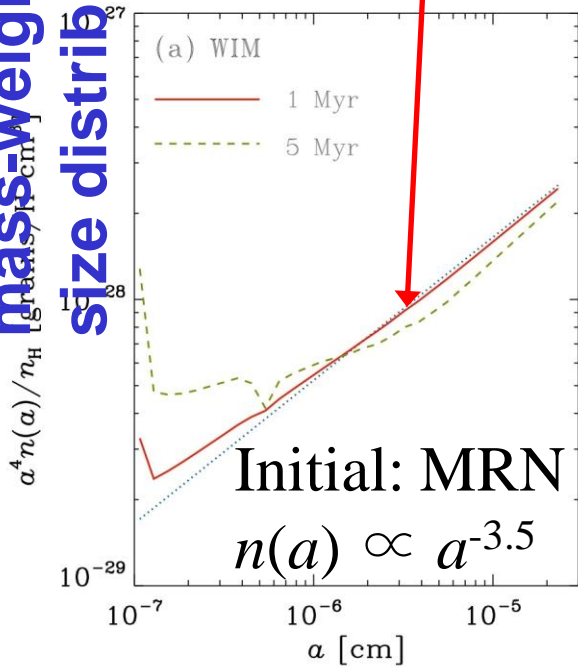
# Results

mass-weighted  
size distribution

Shattering of large grains  
on a short timescale

Upper limit?

Small grains are  
strongly depleted.



Warm ionized medium

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$n_{\text{H}} = 0.1 \text{ cm}^{-3}$

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Warm neutral medium

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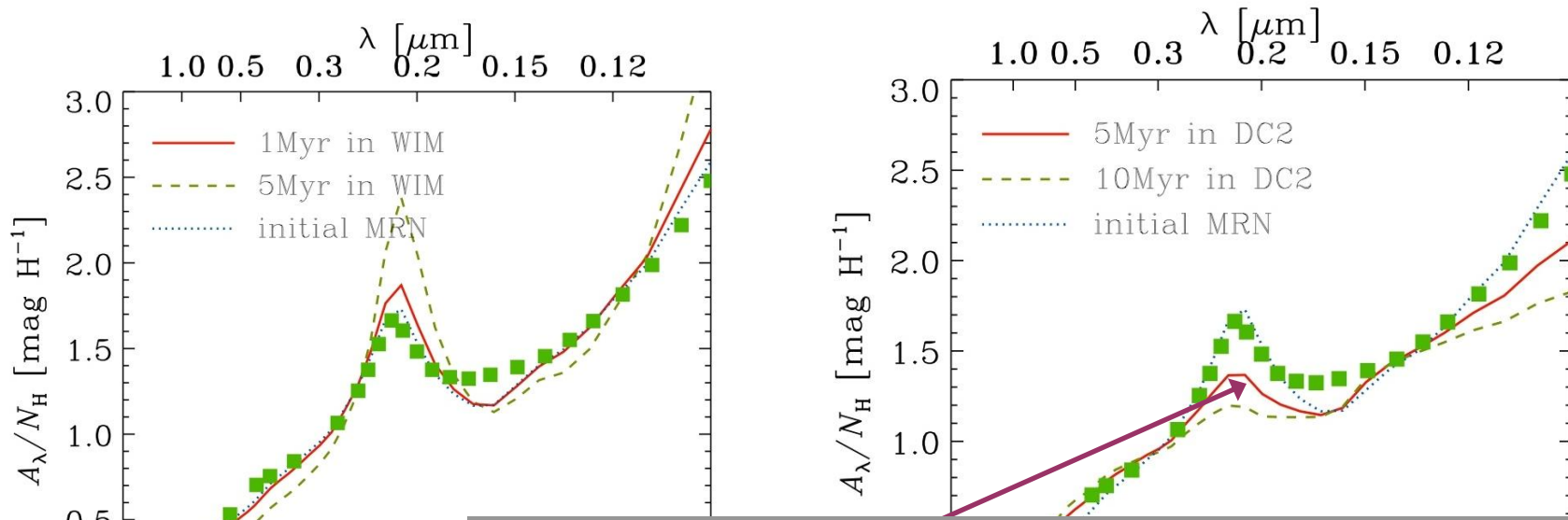
Dense cloud

$T = 10 \text{ K}$

$n_{\text{H}} = 10^4 \text{ cm}^{-3}$

$B = 80 \text{ } \mu\text{G}$

# Effects on the Extinction Curves

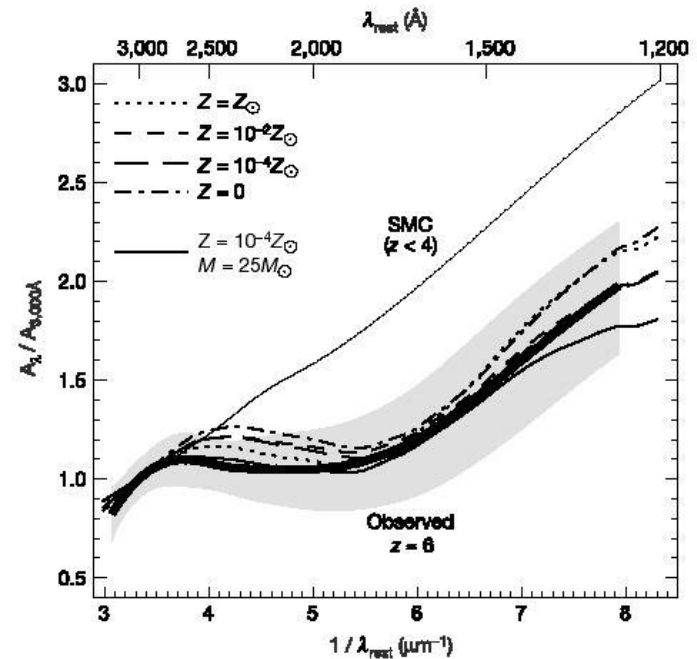
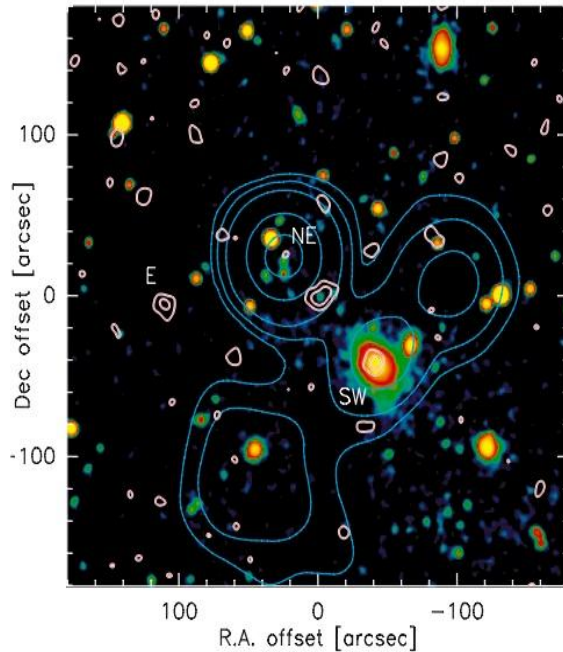


- (1) The UV slope of the extinction curve is sensitive to the bump strength in the grain size distribution in a certain sense.
- (2) The central position of the carbon bump is sensitive to the grain size distribution.
- (3) Small variations in the grain size distribution lead to large variations in the IR extinction curve.

**Shattering and Coagulation in ISM can regulate the grain size distribution (and the extinction curve).**



# 4. In a Cosmological Context

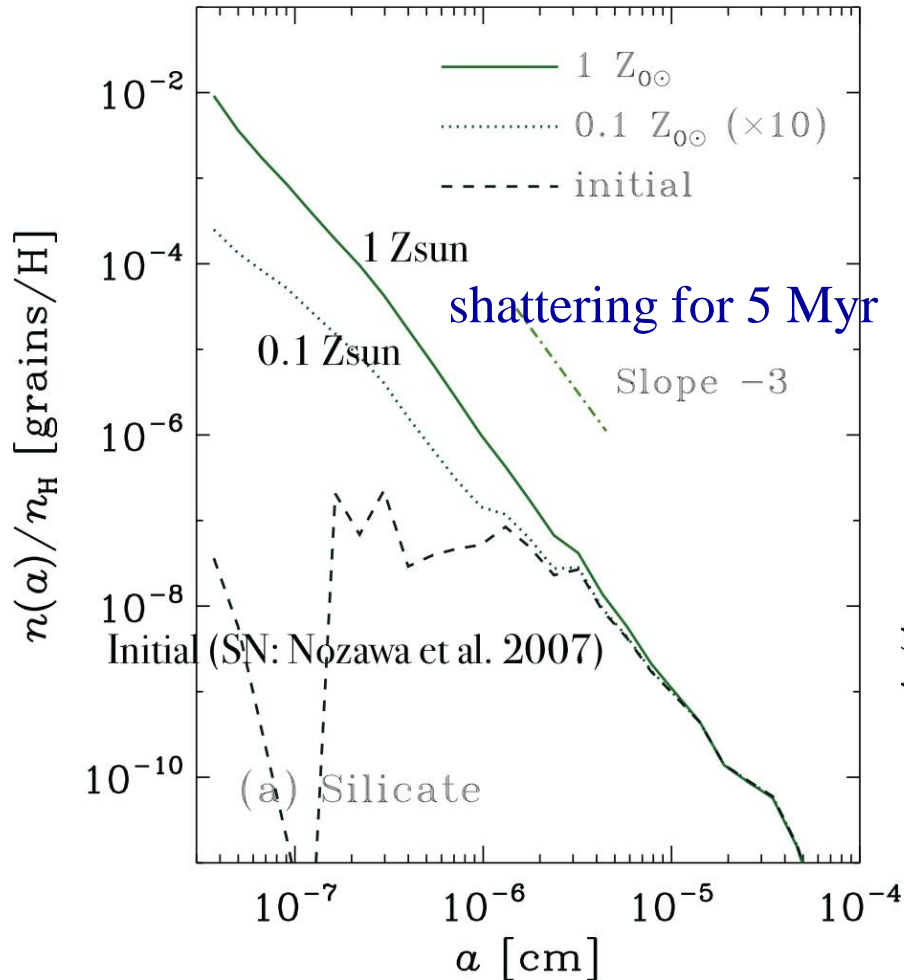


Dust already existed at  $z \sim 6$  (Bertoldi et al. 2003).

Extinction curve at  $z \sim 6$   
Maiolino et al. (2004)

Suggesting a rapid dust enrichment by supernovae

# Shattering of SN Dust

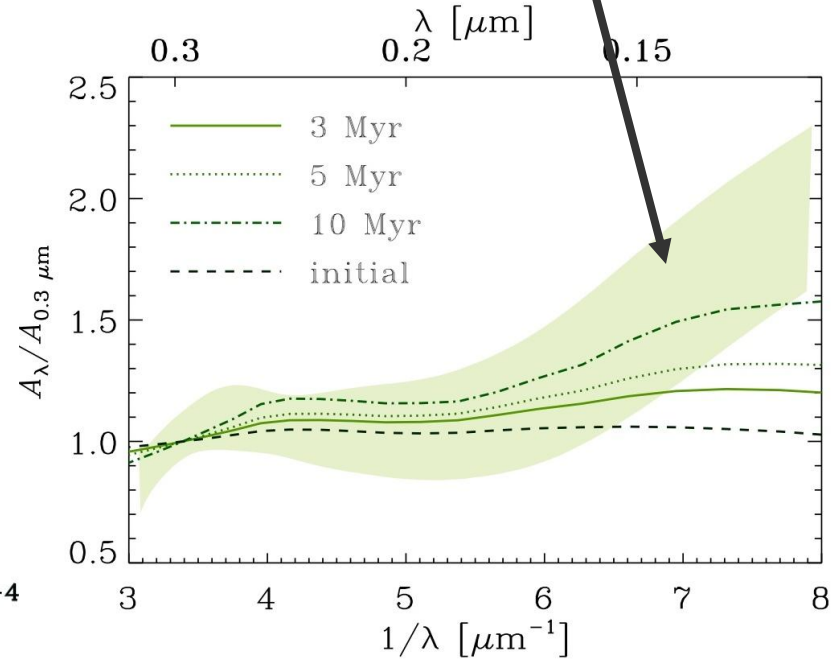


Hirashita et al. (2010)

Hirashita (2010)

extinction curve at  $z = 6.2$

(Maiolino et al. 2004)



Small grain production by shattering contributes to the steepness of the UV extinction curve (in solar metallicity).

# Scenario as a Summary

- (1) The grain size distribution in the formation by supernovae (or AGB stars) **is not processed by turbulence if the metallicity is  $\ll 1/10 Z_{\odot}$ .**
- (2) After the metallicity enrichment, **grain processing in ISM should be considered.**
- (3) In considering the origin of the grain size distribution at the present cosmic age, **interstellar processing by turbulence should be important (occurs everywhere → easy to explain the universality).**

**Thank you.**

# 3. Effects of Coagulation on SF

Hirashita & Omukai (2009)

(1) How about the denser regime?

(2) Importance of dust grains in star formation:

A)  $\text{H}_2$  formation ( $\text{H}_2$  is an efficient coolant for  $Z < 0.01 Z_\odot$ )  $\Rightarrow$  **The grain surface  $S$**  is important.

B) Dust cooling  $\Rightarrow$  **The grain opacity  $\kappa_p$**  is important.

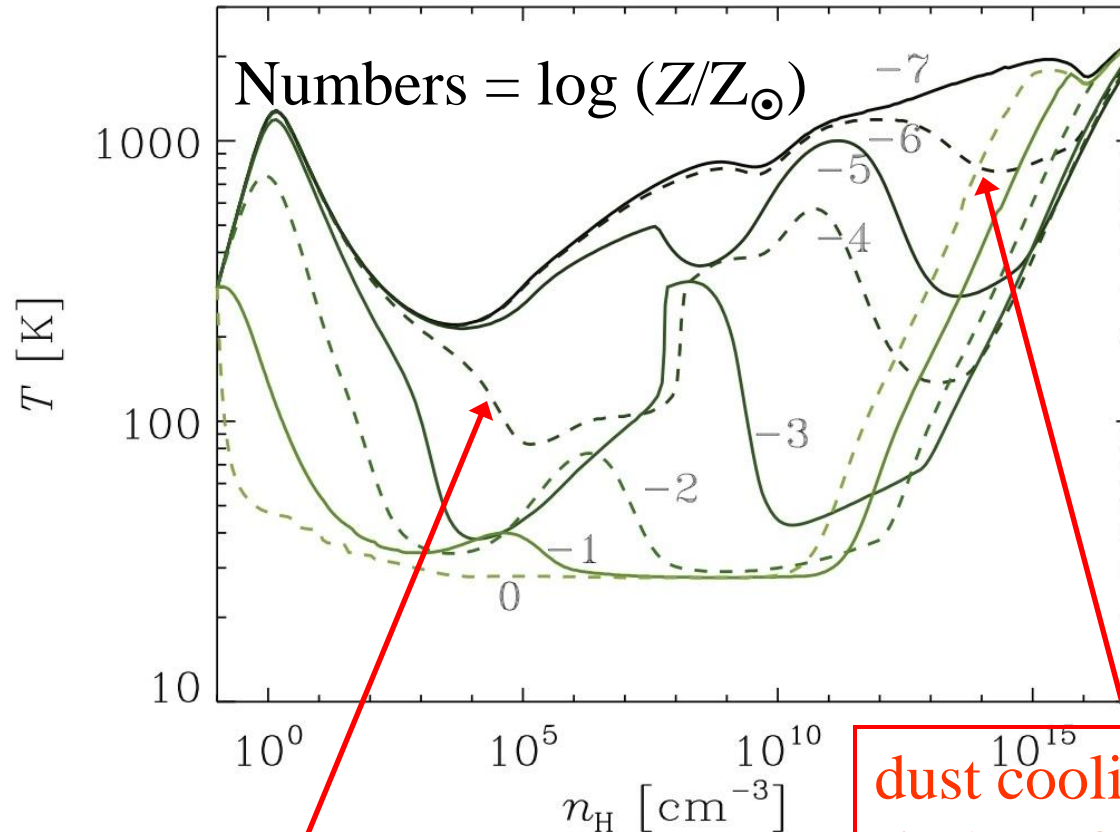


**We calculate the variation of  $S$  and  $\kappa_p$  in star-forming (collapsing) clouds.**

Grain motion is assumed to be thermal.

# Gas Evolution in Collapsing Clouds

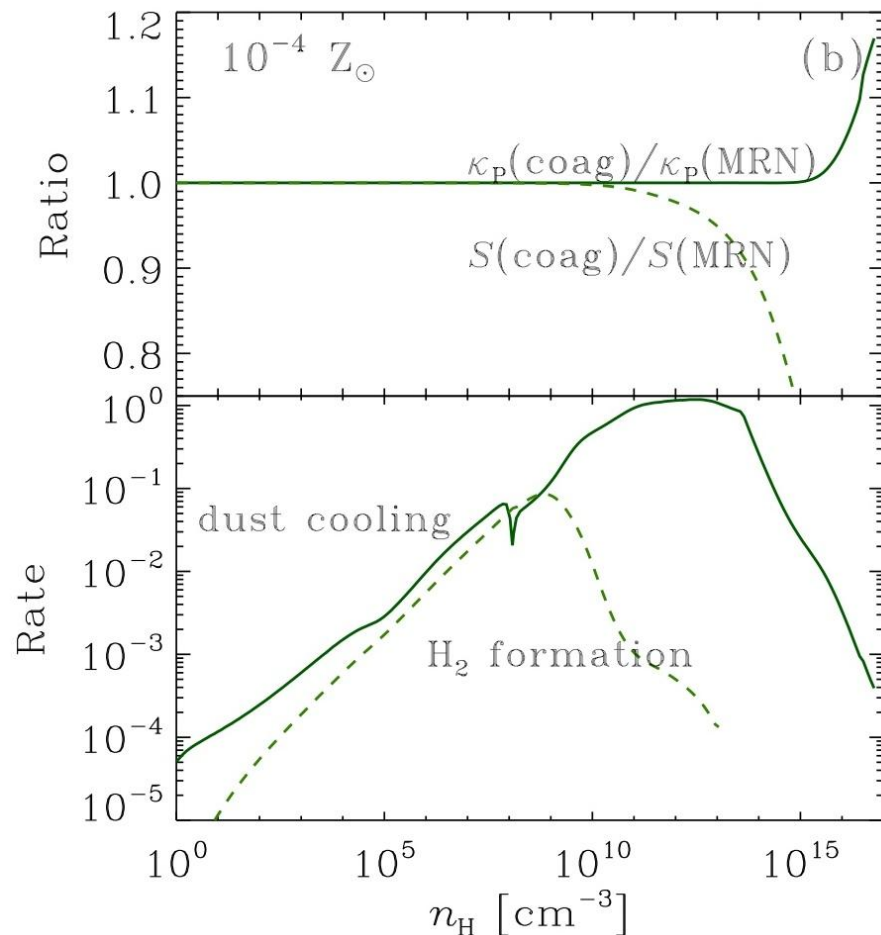
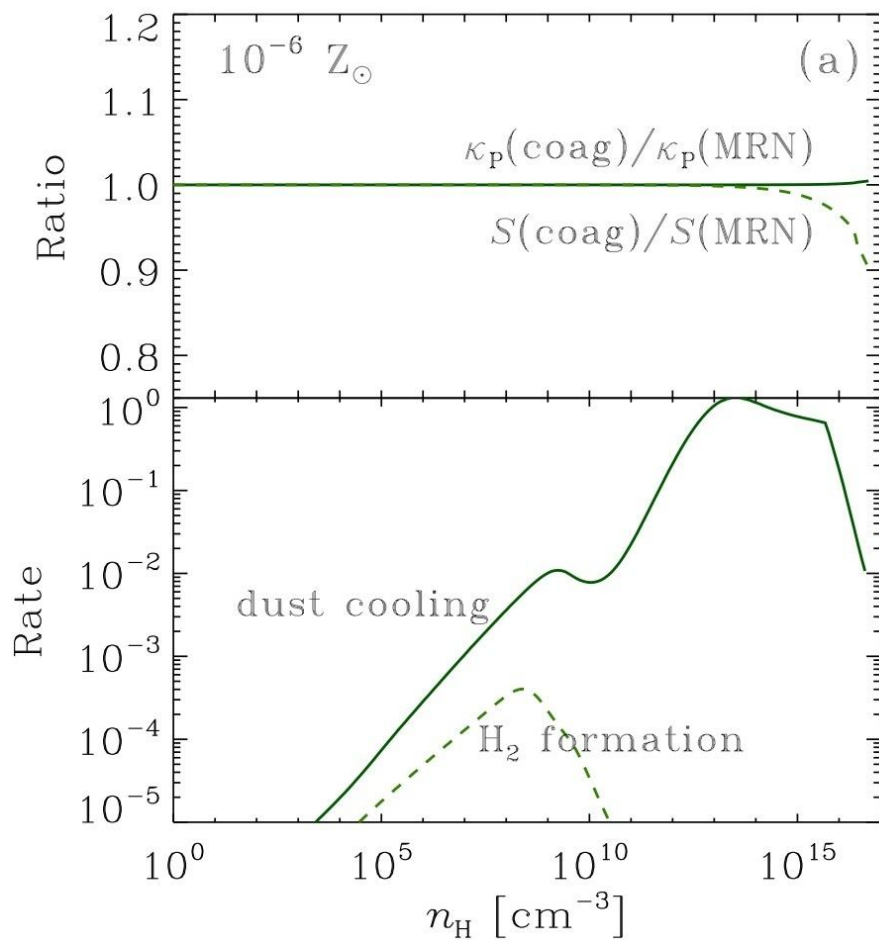
Omukai et al. (2005)



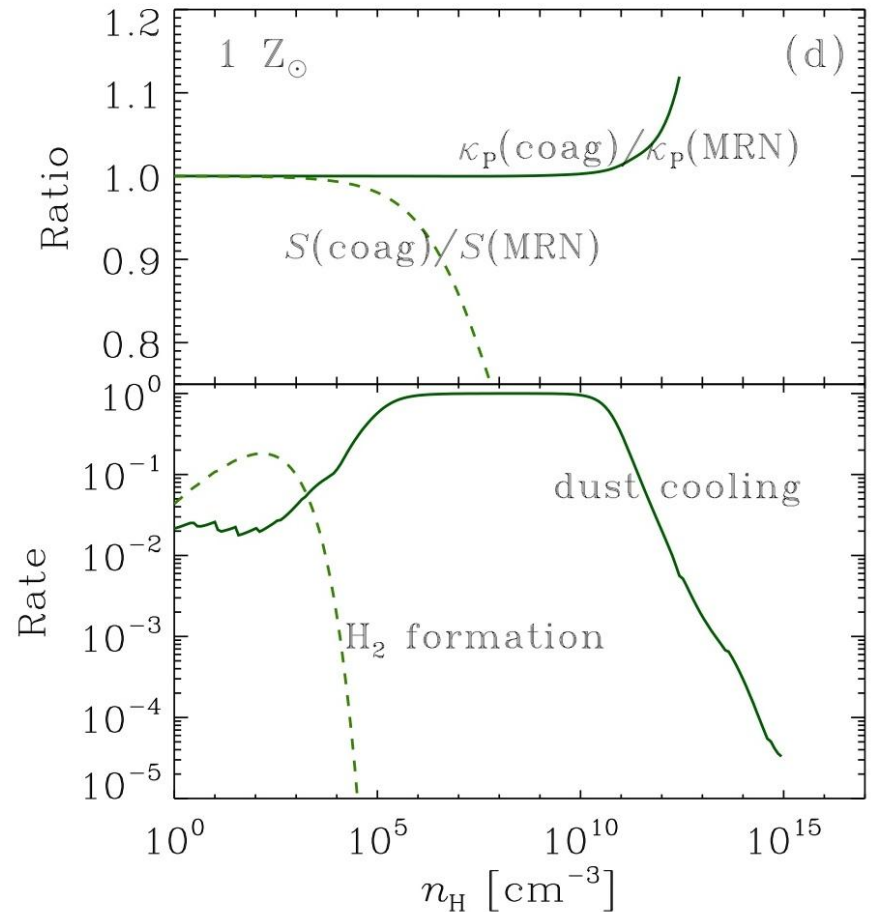
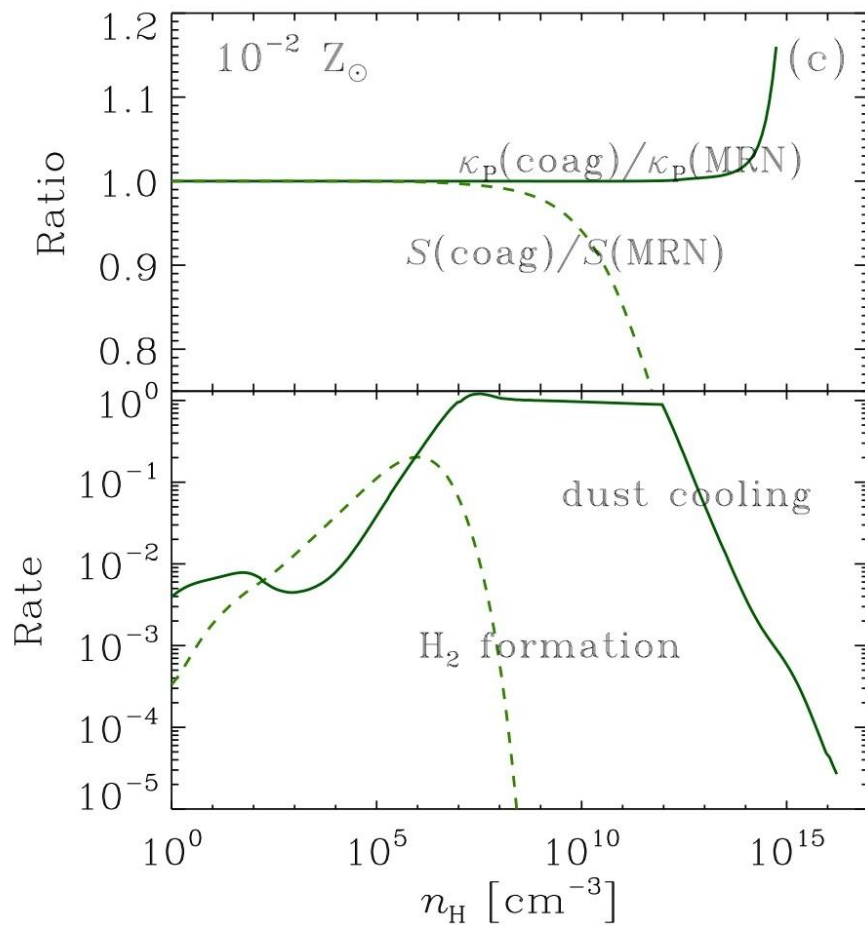
$\text{H}_2$  formation on grain surface:  
important coolant for  $\log(Z/Z_{\odot}) < -2$

dust cooling  
(induce fragmentation)  
Omukai et al. (2005)  
Schneider et al. (2004)

# Change of Grain Surface and Opacity by Coagulation



# Change of Grain Surface and Opacity by Coagulation



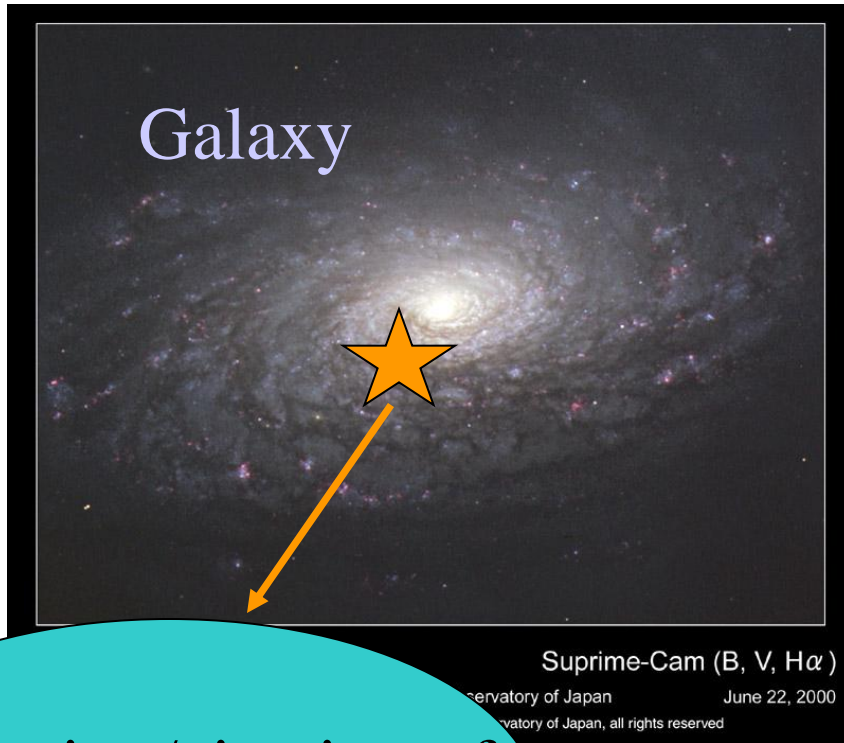


# Physical Considerations

- ☆ Grain surface is dominated by small grains. → Once the smallest grains are affected by coagulation,  $S$  begins to decrease (however,  $H_2$  formation occurs faster).
  - $t_{\text{ff}} > t_{\text{coag}} \Leftrightarrow n_{\text{H}} > 10^7 (Z/Z_{\odot})^{-2} (T/30 \text{ K})^{-1} \text{ cm}^{-3}$
- ☆ Opacity ( $\kappa_{\text{p}} \propto \pi a^2 Q_{\lambda} \propto a^3$ ) is only a function of mass as long as  $a \ll \lambda$ .  $\Rightarrow \kappa_{\text{p}}$  does not change even if coagulation proceeds.

**Coagulation has no effect on the thermal evolution in protostellar collapse.**

# 1. Dust Grains in Galaxies



Formation/ejection of  
heavy elements ( $\geq C$ )

gas, plasma  
(heating by supernovae,  
stellar radiation, etc.;  
radiative cooling)

turbulence  
magnetic fields

Condensation of  
dust grains